1	Identifying the origin of groundwater Samples in a Multi-Layer Aquifer System with						
2	random Forest Classification						
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33 Abstract

34 Accurate identification of the origin of groundwater samples is not always possible in complex 35 multilayered aquifers. This poses a major difficulty for a reliable interpretation of geochemical 36 results. The problem is especially severe when the information on the tubewells design is hard to 37 obtain. This paper shows a supervised classification method based on the Random Forest (RF) 38 machine learning technique to identify the layer from where groundwater samples were extracted. 39 The classification rules were based on the major ion composition of the samples. We applied this 40 method to the Campo de Cartagena multi-layer aquifer system, in southeastern Spain. A large 41 amount of hydrogeochemical data was available, but only a limited fraction of the sampled 42 tubewells included a reliable determination of the borehole design and, consequently, of the 43 aquifer layer being exploited. Added difficulty was the very similar compositions of water 44 samples extracted from different aquifer layers. Moreover, not all groundwater samples included 45 the same geochemical variables. Despite of the difficulty of such a background, the Random 46 Forest classification reached accuracies over 90%. These results were much better than the Linear 47 Discriminant Analysis (LDA) and Decision Trees (CART) supervised classification methods.

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From a total of 1,592 samples, 805 proceeded from one unique identified aquifer, 403 proceeded from a possible blend of waters from several aquifers and 279 were of unknown origin. Only 468 of the 805 unique-aquifer samples included all the chemical variables needed to calibrate and validate the models. Finally, 107 of the groundwater samples of unknown origin could be classified. The uncertainty on the identification of training samples was taken in account to enhance the model. Most of the samples that could not be identified had an incomplete dataset.

54 Keywords: Multi-layer aquifer, Longscreen boreholes, Machine Learning, Random Forest, 55 Hydrogeochemistry, Hydrogeology.

56

57 1. Introduction

58 In complex multi-layer groundwater systems, the correct determination of the origin of a sample 59 is the basic driving condition for a reliable interpretation of geochemical and hydrodynamic 60 results. However, if there is no available information on the tubewell design, this driving 61 condition can be hard to validate (Mayo, 2010). As a consequence, despite the large quantities of 62 geochemical and piezometric data available, only those corresponding to fully documented 63 tubewells should be used for investigation. Hence, there is a need for a tool that could provide an 64 automatic and accurate estimation of the aquifer layer from which a water sample has been 65 extracted. A possibility is to base this tool on geochemical criteria. Such a method must deal with 66 additional difficulties as similar water types, temporal changes in the origin of groundwater, or 67 having different ions analyzed in different samples. Moreover, it should be applicable with 68 common major ion geochemistry. Such a tool could be helpful to all applications of geochemical 69 data in Hydrogeology, as identifying anthropogenic transformation (e.g. Celle-Jeanton et al., 70 2009), understanding paleoclimates (e.g. Jiráková et al., 2009), determining mineralization 71 processes (e.g. Gillon et al., 2012; Lorenzren et al., 2012), assessing groundwater flow patterns 72 (e.g. Cronin et al., 2005) or calibrating groundwater flow models (e.g. Dahan et al., 2004), among 73 other uses.

Statistical methods have been widely used in hydrology and hydrogeology (e.g.; Adams et al., 2001; Lambrakis et al., 2004; Cloutier et al., 2008; Daughney et al., 2012). Generally, as a tool to subdivide and classify large hydrogeochemical datasets to facilitate interpretation. They might also be used to estimate mixing proportions (e.g. Valder et al., 2012). The techniques most applied are principal components analysis (PCA) and hierarchical cluster analysis (HCA). These techniques highlight tendencies inside groups of samples, allowing an easier representation of the results. However, these methods show several limitations, like the subjectivity of the criteria
defining the classes, or its unsupervised nature. That is, they can be used to create a set of classes
out of the whole dataset but they cannot assign samples to a set of a priori classes.

In contrast, in the supervised classification approach, the prediction of the output class of any new sample is enabled by a set of decision rules (classification model) defined out of a set of labeled training samples. This approach enables the prediction of the correct output class for any new input case including the same predictor variables. Linear Discriminant Analysis (LDA) is a classical multivariate technique for supervised classification (Vaselli et al., 1997).

However, traditional statistical methods have been proven inadequate to identify complex
patterns and relationships that could be revealed by more sophisticated procedures (De'ath and
Fabricius, 2000). These new procedures include computer intensive machine learning techniques
based on recursion, sampling and randomizations (Babovic, 2005, Prasad et al., 2006).

92 Approaches based on decision trees (Breiman et al., 1984) are among the most applied supervised 93 classification methodologies. Random Forest (Breiman, 2001), is the one that have recently 94 received most interest. It combines a large numbers of decision trees (usually 500 to 2000) to 95 obtain a more accurate classification without overfitting the model to a specific dataset.

96 Studies using Decision Trees can be found in Remote Sensing (e.g. Guhimre et al., 2010), 97 Medicine (e.g. Lempitsky et al., 2009), Genetics (e.g. Cutler and Stevens, 2006), Chemistry (e.g. 98 Svetnik et al., 2004), Ecology (e.g. Cutler et al., 2007) or Soil Science (e.g. Schmidt et al., 2008). 99 Only a few studies use supervised classification methods in Hydrogeology. Use of decision trees 100 as a supervised classification method has been limited to the studies by Loos and Elsenber (2011) 101 on the links between overland flow generation and topography, and by Peters et al. (2008) on 102 groundwater-dependent vegetation patterns. LDA has been applied to classify groundwater 103 samples only in rare occasions (e.g. Lambrakis et al., 2004). Other machine learning methods as 104 Neural Networks can be found in Hydrogeology (e.g. Kurtulus and Razack, 2007), but they are 105 more difficult to calibrate and were not used in the present study. Except the recent studies by 106 Smith et al. (2010) on bacterial source tracking in lakes and Olson and Hawking (2012) on 107 stream base-flow water chemistry, we have not been able to find any studies using Random 108 Forest neither in Hydrogeology nor for the analysis of hydro-geochemical datasets.

Our main goal was to test the Random Forest classification method to determine the origin of groundwater samples based on their geochemistry. The study was conducted in an intensively irrigated region with hundreds, many of them undocumented, tubewells. These tubewells provide a large geochemical dataset whose interpretation is hazardous due to the lack of designinformation. Linear discriminant analysis and a simple classification tree were also used to compare results.

115 **2.** Study site

116 The Campo de Cartagena, in southeastern Spain (Figure 1), is a 1,440 km² coastal plain whose 117 elevation ranges between 0 and 200 m a.m.s.l. The climate is semiarid with an average 118 temperature of 18 °C and an average rainfall of about 300 mm per year. High variability is 119 another characteristic of precipitation. Several years have registered values lower than 200 mm 120 and, at the same time, more than 150 mm can be registered during a few days, mainly in spring 121 and autumn. The main consequence is the lack of permanent watercourse, though several 122 ephemeral streams drain the area. Groundwater and the Tagus-Segura water transfer, initiated in 123 1980 to derive water from the Tagus basin to the Segura basin, are the main sources of water 124 supply (Baudron et al., 2013).

The economy of the area relies on the agro-industrial sector with crops covering 1/3 of the total surface. Due to the low precipitation rate and a lack of permanent surface water, intensive irrigated agriculture has historically been mainly supported by groundwater extraction from the regional multi-layer aquifer system.

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Figure 1 : Map of the Study Area, with the location of all registered wells and the geological
cross-section of Figure 2.

132

133 2.1. Hydrogeological settings

134 The Campo de Cartagena area corresponds to a Neogene-Quaternary sedimentary basin located 135 on the eastern part of the Betic Cordillera. The permeable sedimentary deposits, with a maximum 136 thickness of 2,000 m, created one of the most important aquifers of the Mediterranean basin 137 (Margat and Vallée, 2000). The main geological and hydrodynamic characteristics of the area, 138 detailed by Jiménez-Martínez et al. (2012), are summarized hereafter. From the Tortonian to the 139 Quaternary, several layers of high-permeability rocks (limestones, sands and conglomerates) 140 were deposited (Figure 2), interlayered with detrital, low-permeability marls. Sands and 141 conglomerates of Tortonian age, organic limestones of Messinian and sandstones deposited 142 during the Pliocene form the three confined layers of the aquifer. The detrital Quaternary 143 sediments form the upper unconfined aquifer. A fifth aquifer, corresponding to slightly evolved 144 Triassic limestone from the substratum, appears locally. A small compartment of the Pliocene 145 aquifer in the Northeastern part, is isolated of the rest of the system by a normal fault. It

All layers are intensively exploited by agriculture, with a maximum estimated extraction of more than 200 hm³ per year with high temporal variability. Natural recharge is scarce and depends on the extent of the layer's respective outcrop areas. Underlying the crops, the Quaternary aquifer is mainly recharged by the irrigation return flow.

More than 40 years of groundwater survey by the Geological Survey of Spain (Instituto Geológico y Minero de España, IGME) provide a large quantity of geochemical and piezometric data, covering a large spatio-temporal range. Nevertheless, due to the lack of design information for most tubewells, the origin of groundwater samples is usually unclear. Identifying representative samples from each aquifer layer, a basic step for any hydrogeological study, is a difficult task.

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157 Figure 2 : A-A' Geological cross-section of the study area.

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3. Dataset and Methods

160 **3.1. Geochemical dataset**

The first step in building a supervised classification model is to collect and prepare a "learning" or "training" dataset to be analyzed. It is used to learn how the value of a qualitative variable, or « target variable » (here, the aquifer layer) is related to the values of a set of « predictor » variables (here, the geochemical ions).

165 **3.1.1.** Collecting data

166 The dataset was obtained by collecting geochemical data from a wide variety of sources. More 167 than 80% of the data came from the official groundwater quality surveys performed between the 168 early 1970s and early 2000s by IGME. Complementary data was provided by the River Segura 169 Basin Authority (Confederación Hidrográfica del Segura, CHS), in several sampling campaigns 170 from 2005 to 2008 and from 2010 to present. Additional geochemical results came from research 171 projects conducted by the Universities of Granada (2009, unpublished data), the University of 172 Murcia (2009 and 2011, unpublished data) and the IDES laboratory of the Paris Sud University 173 (2011, unpublished data). Data from unpublished IGME reports and groundwater analysis kindly 174 eased in the field by wells owners was also included. Finally, the dataset was composed by 1,592 175 groundwater samples (Table 1) collected over a wide range of years, sampling conditions and 176 analytical means and corresponding to different aquifer layers. Most boreholes of the study area 177 are undocumented and were constructed by private owners on their own initiative. Therefore, 178 determination of the borehole design is only available for 300 (15%) of the boreholes. In order to 179 check the descriptions, these 300 boreholes were reviewed in the field.

180 **3.1.2.** Review of borehole-design information

In order to determine the original aquifer of each sample, we collected and reviewed all available borehole-design information corresponding to more than 1200 tubewells in the area. Most data came from the last inventory of wells by IGME, started in 1973 and partly updated at the beginning of the 1980s. Complementary partial inventories (e.g. Conesa-García, 1990) were added, as well as technical reports provided by well owners and drilling companies. The review of the data was based on the following criteria: depth, localization of the screen, presence of a cement ring, age and state of conservation of the tubewells, and the water table evolution (when available). No geochemical criterion was considered. Finally, we could establish that 805 out of a
total of 1,592 groundwater samples came from a single identified aquifer layer (Table 1).

Based on the criteria of the above-described data review, we established an Aquifer Reliability (AR) to weight the reliability of the aquifer assessment for each tubewell. Three levels were defined: A (high reliability), B (medium reliability) and C (low reliability). This index did not take into account any chemical data, but only construction criteria. Indeed, this review of the inventory of wells highlighted that some previous hydrogeological studies could have relied on partially inappropriate aquifer assessment, leading to hazardous interpretations.

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3.1.3. Water types

Based on the 805 samples assigned to just one aquifer layer, the geochemical water-type of each aquifer can be assessed. The Piper diagram for samples with high and medium degree of reliability (AR=A and AR=B) is presented in Figure 3. The Tortonian and Triassic aquifers are well differentiated, with Mg-Na-HCO3 and Ca-SO4 water types, respectively. Nonetheless, the Quaternary, Pliocene and Messinian aquifer are all included in the same Na-Ca-Cl to mixed-Cl water type.

This similarity between water types is a strong limitation to the identification of the characteristic geochemical signature of the three upper aquifer layers. Hypotheses to explain this situation are based on: i) the quite similar geological composition of the aquifer compartments, responsible for a similar mineralization of groundwater (confirmed by similar saturation rates); ii) the irrigation return-flow to the Quaternary aquifer, mixing water coming from the lower layers into the upper ones; and iii) the inside-borehole mixings between water masses (Jiménez-Martínez et al., 2011), which could even have reached a regional scale.

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210 The 805 samples from a single identified aquifer were used to calibrate the model. The model 211 was then used to estimate the aquifer of origin of the 279 samples (Table 1) for which no design 212 information was available and had a complete dataset. The geochemical ions (thereafter called 213 variables) selected to perform the classification are the concentrations (expressed in mg/l) of Cl-. 214 SO42-, HCO3-, NO3-, Ca2+, Na+, Mg2+, K+ and SiO2. One of the problems encountered was 215 that the 8 concentrations were not measured in all the samples. Only 468 of the 805 labeled 216 samples included all the variables needed to calibrate and validate the models (Table 1). Minor 217 and trace elements were not taken in consideration due to the very limited number of samples 218 featuring their determination.

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Figure 3 : Piper diagram for the training samples from single identified aquifer tubewells
with AR=A. 1=Quaternary, 2=Pliocene, 3= Messinian, 4=Tortonian, 5=Triassic.

222

223 **3.2.** Models used

224 **3.2.1.** Linear Discriminant Analysis (LDA)

LDA (Vaselli et al.,1997) is one of the most simple methods for supervised classification. It is used to classify samples into mutually exclusive groups on the base of independent variables. This objective is attained by maximizing the between-group variance and minimizing the withingroup variance. It is closely related to the unsupervised principal component analysis (PCA) in that they both look for linear combinations of variables that best explain the data. An important assumption of LDA is that the independent variables are normally distributed. If only two variables are available, the separators between the groups will become lines. If three variables are available, the separator is a plane. When the number of variables is higher than three, theseparators become a hyper-plane.

234 **3.2.2.** Decision Trees

235 Decision trees are used to build a model by a recursive binary partition of a labeled dataset into 236 increasingly homogeneous nodes. Homogeneity is measured with the Gini index (Breiman et al., 1984), defined as $G = \Sigma k p_k \cdot (1 - p_k)$, where p_k is the proportion of observations in the kth class. 237 238 This index is minimized when all observations belong to the same class. At each step the node 239 with the highest G value is split; a an optimization is done to select the predictor variable and the 240 numeric threshold, or group of values is the variable is categorical, that would produce the lowest 241 G value in the subsequent nodes The splitting process continues until no further subdivision can 242 reduce the Gini index (Cutler et al., 2007).

243 The final result should be a fully-grown classification tree whose lower nodes include cases 244 belonging to just one class. However, the lower nodes are seldom, if ever, completely 245 homogeneous. In this case, the predominant class is used to label the node, being the other cases 246 classification errors. On the basis of these errors it is possible to prune the tree to allow a higher 247 generalisation capacity. A typical pruned classification tree has 3 to 12 terminal nodes. This 248 trained decision tree can then be used to classify an unlabeled dataset. Interpretation of 249 classification trees increases in complexity as the number of terminal nodes increases (Cutler et 250 al., 2007).

251 **3.2.3.** Ensemble Learning

The main problem of classifying with a unique tree is its high sensitivity to the input data, small modifications in the dataset can produce completely different models. Ensemble Learning techniques have recently received much interest as a tool to overcome this limitation of decisiontrees, to obtain better predictive performance.

256 Bagging (Breiman, 1994) is one of the most used ensemble learning methods. It generates 257 independent trees by re-sampling the same dataset by bootstrapping. That is generating new datasets of the same size as the initial one by random sampling with replacement. Around 67% of 258 259 the original observations occur at least once in each new generated dataset. Observations not 260 included in any of the new datasets are called "out-of-bag" observations. The trees obtained are 261 not pruned and are used to classify the out-of-bag observations. As each initial observations is 262 included inside the out-of-bag of several trees, its class is estimated several times. The final 263 estimation assigns each observation to the most "voted" class (Liaw and Wiener, 2002).

264 **3.2.4.** Random Forest (RF)

265 Random Forest (RF) is a bagging based method proposed by Breiman (2001). It generates several 266 trees (500 to 2,000) using bootstrapping; each tree is then trained using a randomized subset of 267 the predictors. This somewhat anti-intuitive modification adds randomness to bagging and 268 decreases the correlation between trees. Uncorrelation is a desiderable property in ensemble 269 learning classifiers to guarantee that different results give sense to the voting system. Random 270 Forest produces very good results compared to other machine learning based classification 271 systems (Support Vector Machines or Neural Networks) or to other decision tree algorithms 272 (Breiman, 2001; Liaw and Wiener, 2002).

Random Forests do not overfit the model to the dataset since the classification error of one
permutation can be overcome by the ensemble of permutations (Ghimire et al., 2010). This way
the large number of trees reduces generalization error (Breiman, 2001; Pal, 2005; Prasad et al.,

13

276 2006). Since the out-of-bag observations are not used in the fitting of the trees, the out-of-bag 277 estimates can be used to perform a cross-validation accuracy estimation (Cutler et al., 2007).

278 One of the parameters that can be set up by the user is the number of variables included in each 279 classification tree. Nevertheless, the method does not seem to be very sensitive to this value, 280 which is by default the square root of the total number of variable used (Gislason et al., 2006). 281 Another user configurable parameter is the number of generated trees, although a higher number 282 does not seem to provide a substantial increase in the classification accuracy (Liaw and Wiener, 283 2002). In general, random forests do remarkably well and require very little tuning (Hastie et al., 284 2003).

285 A disadvantage of Random Forest compared to the simple classification tree approach is that 286 individual trees cannot be examined separately, thus becoming a "black box" approach (Prasad et 287 al., 2006). However, it does provide several metrics that help in interpretation. Variable 288 importance is evaluated based on how much worse the prediction would be if the data for that 289 predictor were permuted randomly. The resulting values can be used to compare relative 290 importance among predictor variables. In this way, the procedure is much more interpretable than 291 methods such as Neural Networks, and it has been called a "grey box" approach (Prasad et al., 292 2006).

293

3.2.5. Validation

294 Random Forest includes its own cross validation procedure (out-of-bag cross validation). While 295 some authors consider it unnecessary to perform a separate cross-validation (Efron and 296 Tibshirani, 1997; Breiman, 2001; Svetnik et al., 2004), others like Mitchell (2011) affirm that this 297 internal cross validation can generate biases in the classification. Although it is computationally more intensive, we preferred to perform a separate leave-one-out cross validation to compare
Random Forest results with other methods' (LDA and decision trees) with the same validation
tool.

301 The results of a cross-validation are organized in a confusion matrix (Table 2) where columns (i)302 correspond to real classes, and lines (i) show the model results. Each element of the n_{ii} matrix 303 represents the number of observations corresponding to class *j* that were classified as class *i*. 304 Several indices measuring the accuracy of the classification can be generated from the confusion 305 matrix (Congalton and Green, 2008). The overall accuracy is the proportion of cases in the 306 principal diagonal. The omission error of class i is the proportion of cases from class i not classified as such. The commission error of class *i* is the proportion of cases incorrectly classified 307 308 as class *i*. Finally, the kappa index corrects the overall accuracy for random chance agreement as 309 detailed in Congalton and Green (2008):

$$K = \frac{n \sum_{i=1}^{J} n_{ii} - \sum_{i=1}^{J} n_{i+} n_{+i}}{n^2 - \sum_{i=1}^{J} n_{i+} n_{+i}}$$

310

311 **3.3.** Formulation of tested models

A general schema of the methodology used in this study is shown in Figure 4. Five models weretested:

- 314 1. Linear Discriminant Analysis (LDA)
- 315 2. Classification Tree using the CART algorithm (CART)
- 316 3. Random Forest (RF0)
- 317 4. Random Forest eliminating unreliable samples (RF1)
- 318 5. Random Forest eliminating variables to increase accuracy (RF2)

319

Several algorithms to apply classification tress have been proposed. In this study we have used
the Classification and Regression Trees (CART) proposed by Breiman et al. (1984).

Model RF1 was an attempt to increase the accuracy of the results by the detection and elimination of unreliable samples (Figure 4). Two strategies were applied. First, the ionic balance for each water sample was calculated to determine if errors in classification could be related with errors in the balance. Secondly, we considered the qualitative evaluation of the reliability of the initial aquifer assessment (AR) for each borehole. As for the previous case, the aim was to assess whether unreliable ground water samples decreased the accuracy of the classifications.

328 6. The purpose of model RF2 was to deal with

329 the decrease in accuracy observed when the number of variables reaches a certain threshold. This 330 phenomenon is known as Hugues effect, or Curse of Dimensionality (Hugues, 1968). It can be 331 attributed to a significant reduction of the sample density in the space of variables as the increase 332 in the number of variables is not compensated by an increase in the sample size. Several models 333 were built to analyze this phenomenon and check its effects. We started with the simplest model, 334 with only the most important variable, using Random Forest variable ordination. Then, we added 335 the variable that most increased the accuracy of the model. Because of the random behavior of 336 the Random Forest, the selection of this variable was not based on only one classification but on 337 50 different classifications of each new generated model. Thus, we obtained the corresponding 338 distribution of accuracy parameters, in this case calculated using out-of-bag cross-validation 339 instead of leave-one-out cross validation to save computing resources and because in this case 340 different Random Forest results are being compared. Using a similar procedure, the other variables were progressively added. The expected result was a fast increase in accuracy when
adding the first variables, followed by a stabilization or even a decrease in accuracy, due to the
Hugues effect with the incorporation of the less important variables.

344 **3.3.1**.

345

The work was carried out with the R programming language (R Development Core Team, 2010)
using the R packages *rpart* (Therneau et al., 2011) and *randomforest* (Liaw and Wiener, 2002)
that implement the CART and Random Forest algorithms, respectively.

349 Figure 4 : Methodological scheme

350

351 4. **Results and discussion**

352 4.1. Linear Discriminant Analysis (LDA)

Table 3 shows the results of the LDA classification. Overall accuracy reaches 84.8% with a kappa index of 0.764. Despite of these significantly high values, omission and commission errors reach 100% for the Pliocene aquifer. This means that no sample from the Pliocene was classified as such and that all samples classified as Pliocene were incorrectly classified.

357 4.2. Classification and Regression Trees (CART)

According to the confusion matrix (Table 4), the results are quite good, with an overall accuracy of 88%. As for LDA, the omission error reaches 100% in the case of the Pliocene aquifer; 360 however, the commission error was 0%, meaning that no sample was classified as Pliocene.

361 In the decision tree produced (Figure 5), each one of the 8 internal nodes is defined by a 362 condition. The sample continues on the left branch if this condition is fulfilled and on the right 363 branch if not. The 9 final nodes correspond to the 5 layers, except Pliocene which, as has been 364 said, did not receive any observation. Figures 6 to 8 illustrate and explain the main geochemical 365 nodes of the classification tree obtained. They show how the first decision rules split the space of 366 the variables into a set of different subregions corresponding to different aquifers. Another way to display the nodes is to use a binary axis. In the space defined by NO_3^- and Ca^{2+} (Figure 6), a high 367 368 number of Quaternary samples were correctly classified because of NO₃⁻ concentrations above 44 369 mg/l. The number of badly classified samples was 6 from the Pliocene aquifer, 6 from the 370 Messinian and 2 from the Triassic aquifer. One possible explanation could be a mixing with 371 Quaternary water with high contents in NO₃. As well, all samples with less than 44.0 mg/l of NO_3^- and less than 55.5 mg/l of Ca^{2+} are directly classified as Tortonian. These include 92% of 372 373 the Tortonian samples and 3 samples coming from other aquifers, therefore badly classified. The samples with less than 44.0 mg/l of NO_3^- and more than 55.5 mg/l of Ca^{2+} generate two sub-trees 374 375 that are analyzed in Figure 7 and Figure 8. The first sub-tree involves samples with less than 44.0 mg/l of NO₃⁻ and Ca²⁺ between 55.5 mg/l and 277.5 mg/l (Figure 7). The definitive assignation 376 (Messinian or Quaternary) of the samples is based on the Mg^{2+} and Cl^{-} contents. The second sub-377 378 tree (Figure 8) includes three variables: Cl⁻ on the abscissa, HCO₃⁻ on the ordinate and the 379 threshold in Cl⁻, highlighted by the size of the points. Figure 8 also shows how successful the 380 classification in this part of the tree is, with only one error for the Triassic aquifer and three for 381 the Pliocene, probably partly explained by the mixing process cited above.

382 The confusion between Pliocene and Quaternary can be explained by Quaternary nitrate-rich

 $(NO_3^- < 44.0 \text{ mg/l})$ water entering the Pliocene through long-screen boreholes, and in some cases with high Cl⁻ as well. The confusion with the Messinian seems to be linked to the same problem, but it also has to be taken in account that both sample types are located in the same regions of the space of the variables.

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- **388** Figure 5 : Classification tree generated by CART
- Figure 6 : Plot of the $NO_3^- < 44$, $Ca^{2+} \ge 55.5$ and $Ca^{2+} < 277.5$ nodes of the decision tree obtained by the CART model. Note: values in mg/l
- Figure 7 : Plot of the Mg²⁺ < 179.5 and Cl⁻ < 1024 nodes of the decision tree (CART model).
 Note: values in mg/l

393 Figure 8 : Plot of the Cl⁻ >= 716, HCO₃⁻ < 542.5 and K⁺ >= 20.5 nodes of the decision tree

394 (CART model). Note: values in mg/l

395

396 4.3. Random Forest (RF0)

The confusion matrix after applying Random Forest to the whole dataset and all the available variables is shown in Table 5 together with its analysis. Compared to the CART model, overall accuracy increased from 88.0% to 90.6%, i.e. 21.7% of the total scope of improvement. The omission error for the Pliocene aquifer decreased from 100% to 70.0%, showing a clear enhancement, although this value remains high. The commission error for the Pliocene is also high (40.0%). Table 6 shows the importance of each variable according to one of the Random 403 Forest importance criteria: the increase in accuracy provided by this variable to the classification.

404 4.4. Random Forest after elimination of unreliable samples (RF1)

Figure 9 shows the distribution of the ionic balance error (absolute values) for each result of the 405 406 model. The actual and the estimated classes appear separated by a dot on the horizontal axis. 407 Well-classified samples (1.1, 2.2, 3.3, 4.4, 5.5) seem to have a lower ionic balance error than 408 badly classified samples. Nevertheless, overlapping areas between categories are very large, so 409 no clear threshold can be assessed. As a general rule, we decided to eliminate all samples above 410 5% of absolute ionic balance error (2 samples) for the calibration of the model. Anyway, there is 411 a slight tendency to obtain better classifications in samples with a low error in the ionic balance. 412 We think this supports the use of this classification method.

413

414 Figure 9 : Absolute Ionic Balance Error

415

416 Depending on the borehole, the initial aquifer assigned to the samples is more or less reliable. 417 The Aquifer Reliability (AR) expresses three levels of confidence: A (high), B (medium) and C 418 (low). Figure 10 shows the distribution of AR for each one of the 25 possible classification cases 419 (correct and incorrect). It is organised as a confusion matrix in which the elements are pie charts 420 displaying, for each combination of real and estimated classes, AR distribution. The colors are 421 chosen as follows: green (AR="A"), yellow (AR="B") and red (AR="C") while the number in 422 brackets indicates the number of cases. Nine combinations never occur (white circles); for 423 example, samples from the Ouaternary aguifer wrongly classified as Tortonian. In most cases of bad classification, a predominance of low reliability initial aquifer assignment (AR="C") is
found. Specifically for Quaternary and Pliocene samples incorrectly classified as Messinian, most
samples feature a highly reliable initial aquifer assignment (AR="A"). In some cases (Pliocene,
Messinian and Trias), well-classified samples present relatively high percentages of medium and
low AR. In view of these results, it was decided to eliminate the samples featuring low AR.

After eliminating all samples with AR="C", together with those with an ionic balance error higher than 5, the classification accuracy increases (Table 7). Especially relevant is the decrease from 70% to 48% in the omission error of the Pliocene aquifer. The commission error for the same layer reaches a reasonable value of 13.3%. Overall accuracy, increases from 90.6% to 93%.

433

Figure 10 : Distribution of reliability index (ARI) for the different combinations of actual
and classified aquifers

436

437 4.5. Random Forest after elimination of variables (RF2)

To assess if any of the variables was producing a decrease in accuracy, different models were generated by adding and eliminating variables. We started with a model containing only NO_3^- , the variable that had obtained the higher importance in the RF0 model. This one-variable model reached an accuracy of 71%. Then we check which variable produced the highest increase in accuracy. It, turned out to be Ca^{2+} . This two-variable model attained an accuracy of 81%. Continuing step by step with the same procedure, a model including all the variables was obtained (Figure 11). Due to the random behavior of Random Forest, the results can vary from one run to another. Therefore, the protocol was repeated 50 times for each model. The accuracyresults were obtained by out-of-bag cross-validation.

447

448 Figure 11 : Accuracy of different models generated by adding and eliminating variables

449

A decrease in accuracy was observed after adding the last variable (Cl⁻). Eliminating chloride therefore improved the model (Table 8): a reliability of 94.3% was reached with a decrease of the commission error for all classes. Specially important is the decrease in the omission error of the Pliocene aquifer, from 48% to 40%. Removing Cl⁻ also seemed to reduce the confusion between Pliocene and Messinian aquifers.

It is interesting to compare the evaluation of variables given by Random Forest with the decision tree generated by the CART model (Figure 5), In the former, NO_3^- remains as the most important variable, Ca^{2+} and Mg^{2+} maintain a fairly high importance. The main difference is the importance that Random Forest gives to Na^+ and the rejection of Cl⁻ that seems to reduce the confusion between Pliocene and Messinian.

460 4.6. Statistical models comparison

The similarity between water types was initially expected to be a strong limitation to the identification of the characteristic geochemical signatures of the three upper layers. Another problem is that groundwater mixings between aquifer layers are accumulative over time, producing temporal variation in the geochemistry of groundwater samples. Despite such limitations, RF2 model reaches high accuracy and low omission error for the Pliocene compared

466	to the other methods (Figure 12), Therefore, the RF2 model is selected as the best model. Out of
467	the 171 tubewells of unknown design featuring geochemical data, and based on the training set of
468	73 tubewells, it succeeded to identify the aquifer corresponding to 66 tubewells (Figure 13).

469

470 Figure 12 : Accuracy indicators for the different models: LDA, CART, RF, RF1 and RF2.

471 Figure 13 : Map of the RF2 results

472

473 4.7. Predictive capacities of the model

The results of the RF2 model for unknown samples are represented in a Piper diagram (Figure 14). Piper diagrams display geochemical water-types, i.e. the relative proportion of several geochemical species in the total mineralization of a sample. They use slightly different data than the used by Random Forest. First, data appear as percentages whereas the model is built on concentration values; secondly, some of the ions appear added. So, we think that a Piper diagram of the classified samples can be used as a second validation approach and to check the predictive capacity of the model.

The water types displayed on Figure 14 (classified samples) are similar to those showed on Figure 3 (training samples), confirming the reliability of the method to identify the origin of groundwater samples. Two problems, not directly attributable to the model, still appear. Some of the samples could not be identified because not all the ion concentrations had been measured when the samples were collected, making the classification impossible. Secondly, some of the classified samples could actually represent a mixing between different aquifers layers; this
already mentioned phenomenon is characteristic of the study area. Both problems, incomplete
datasets and mixing samples, are to be dealt in future works.

489

Figure 14 : Piper diagram for samples from unknown origin featuring all variables and
identified with the RF2 model. 1=Quaternary, 2=Pliocene, 3= Messinian, 4=Tortonian,
5=Triassic.

493

494 **5.** Conclusions and perspectives

495 Based on training samples featuring all variables, the first two models (LDA and CART) showed 496 overall accuracies of 84.8 and 88.0% (respectively). A high disparity was found between 497 geochemically easy distinguishable aquifer layers (Tortonian, Triassic) and others that present 498 higher geochemical similarity (Quaternary, Pliocene and Messinian). Although these values seem 499 quite acceptable, these models did not succeed to correctly classify any of the Pliocene training 500 samples. With the same dataset, the first Random Forest model (RF) reached slightly higher 501 overall accuracies (90.6%) and succeeded to classify part of the Pliocene samples. The 502 elimination of less-reliable samples, based on both geochemical and tube-well design criteria, 503 provided a stronger Random Forest model (RF1) with exactitude of 93.0%. After eliminating the 504 less useful variables, the final Random Forest model (RF2) achieved an overall accuracy of 505 94.3% and the best classification.

These good results prove that Random Forest allows to identify the aquifer of origin of groundwater samples based on commonly available major ions geochemistry, even when the different aquifer layers have similar geochemical water types. Random Forest also provide more 509 accurate classification than LDA or CART. The identification of the aquifer of origin of unknown 510 samples optimizes the hydrogeochemical dataset, enhancing the possibilities of geochemical 511 interpretations. The results of this study present a wide interest limited neither to this kind of 512 problem nor to the Campo de Cartagena aquifer system. Indeed, many multi-layer aquifer 513 systems feature long-screen boreholes, and could benefit from this methodology to increase the 514 geochemical knowledge. More generally, the Random Forest methodology does show potential 515 for a wide range of hydrological, hydrogeological and geochemical applications, and offers novel 516 prospects in this field.

517 Still, developing several aspects could enhance the present classification model. Firstly, a strategy 518 to identify water samples produced by the mix of groundwater from different layers inside 519 longscreen boreholes would improve the results. Secondly, several samples were not used to 520 calibrate the model because not all the 8 predictor variables had been measured. It would be 521 necessary to check the accuracy of the method with samples with much less information. Thirdly, 522 temporal variability is an accumulative factor that can introduce temporal variation in the 523 geochemistry of samples and, consequently, noise in the models. Finally, the spatial variability of 524 the agricultural activity, and the introduction of NO_3^- in the aquifers, is not the same in the whole 525 area. This spatial variability could be also affecting the models. In forthcoming works, these 526 tracks will be investigated.

527

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- 650
- Table 1: Summary of the groundwater samples included in the dataset. Most samples
 marked with an asterisk (*) did not feature a full set of variables.
- Table 2: Mathematical illustration of a confusion matrix. Adapted from Congalton and
 Green (2008).
- 655 **Table 3 : Confusion matrix of discriminant analysis**
- 656 Table 4 : Confusion matrix of CART classification tree
- 657 **Table 5 : Confusion matrix of random forest**
- **Table 6 : Importance of variables in relation to the corresponding accuracy increase**
- 659 Table 7 : Confusion matrix of random forest eliminating doubtful samples (RF1)
- 660 Table 8 : Confusion matrix of random forest eliminating Cl⁻

Highlights

- Identification of the origin of groundwater samples based on their geochemistry.
- Enhancement of a geochemical dataset featuring doubtful samples.
- Novel application of Random Forest (RF) machine learning technique in hydrogeology.
- High discrimination capacity, beyond similar water types and heterogeneous dataset.
- Optimization of the classification model by assessing the most useful variables.

Figure 1 : Map of the Study Area, with the location of the registered wells and the geological cross-section of Figure 2.

Figure 2 : A-A' Geological cross-section of the study area.

Figure 3 : Piper diagram for the labelled training samples from single identified aquifer tubewells with AR=A. 1=Quaternary, 2=Pliocene, 3= Messinian, 4=Tortonian, 5=Triassic.

Figure 4 : Methodological scheme

Figure 5 : Classification tree generated by CART

Figure 6 : Plot of the $NO_3^- < 44$, $Ca^{2+} >= 55.5$ and $Ca^{2+} < 277.5$ nodes of the decision tree obtained by the CART model. Note: values in mg/l

Figure 7 : Plot of the $Mg^{2+} < 179.5$ and Cl < 1024 nodes of the decision tree (CART model). Note: values in mg/l

Figure 8 : Plot of the $Cl \ge 716$, $HCO_3^- < 542.5$ and $K^+ \ge 20.5$ nodes of the decision tree (CART model). Note: values in mg/l

Figure 9 : Absolute Ionic Balance Error

Figure 10 : Distribution of reliability index (AR) for the different combinations of actual and classified aquifers

Figure 11 : Accuracy of different models generated by adding and eliminating variables

Figure 12 : Accuracy indicators for the different models: LDA, CART, RF, RF1 and RF2.

Figure 13 : Map of the RF2 results

Figure 14 : Piper diagram for samples from unknown origin featuring all variables and identified with the RF2 model. 1=Quaternary, 2=Pliocene, 3= Messinian, 4=Tortonian, 5=Triassic















Mg





Actual aquifer.Estimated aquifer

Figure 10 Click here to download high resolution image













*

Whole dataset	1592			
	Tota	al 805		
Samples from one only aquifer	Featuring all variables 468	With missing variables 337		
	Tota	al 282		
Samples of unknown origin	Identified with RF2 107	Not identified with RF2* 175		
Samples identified as mixing	4	03		

	j=colum	row				
		totals				
		1	2	3	 J	ni+
i=rows	1	<i>n</i> 11	<i>n</i> 12	<i>n</i> 13	 n1J	<i>n</i> 1+
(model	2	<i>n</i> 21	n22	<i>n</i> 23	 n2J	<i>n</i> 2+
class)	3	<i>n</i> 31	n32	<i>n</i> 33	 n3J	<i>n</i> 3+
	Ι	<i>nI</i> 1	nI2	nI3	 nIJ	nI+
tot. column	n+j	<i>n</i> +1	<i>n</i> +2	<i>n</i> +3	 n+J	n

	Q	Р	М	То	Tr
Quaternary	206	7	5	0	0
Pliocene	0	0	1	0	1
Messinian	26	22	130	1	2
Tortonian	1	1	0	24	0
Trias	0	0	4	0	37
Commission error	5.5	100	28.2	7.7	9.8
Omission error	11.6	100	7.1	4	7.5
к=0.764					
Overall accuracy=84.8%					

	Q	Р	М	То	Tr
Quaternary	227	11	11	0	2
Pliocene	0	0	0	0	0
Messinian	5	18	127	2	2
Tortonian	1	1	1	23	0
Trias	0	0	1	0	36
Commission error	2.57	0	10	8	10
Omission error	9.56	100	17.64	11.54	2.7
к=0.809					
Overall accuracy=88%					

	Q	Р	М	То	Tr
Quaternary	225	4	7	0	2
Pliocene	2	9	16	1	0
Messinian	6	16	129	0	1
Tortonian	0	1	0	25	0
Trias	0	0	1	0	36
Commission error	5.46	40	15.13	3.85	2.7
Omission error	3.43	70	7.86	0	10
к=0.853					
Overall accuracy = 90.6%					

ion	NO ₃ ⁻	Mg ²⁺	Na ⁺	Ca ²⁺	Cl	SO4 ²⁻	K^+	HCO ₃	SiO ₂
Overall accuracy	0.270	0.107	0.104	0.098	0.085	0.060	0.051	0.035	0.015

	Q	Р	М	То	Tr
Quaternary	210	3	6	0	0
Pliocene	0	13	2	0	0
Messinian	5	9	72	0	0
Tortonian	0	0	0	25	0
Trias	1	0	0	0	25
Commission error	4.11	13.33	16.28	0	3.85
Omission error	2.78	48	10	0	0
к=0.882					
Overall accuracy = 93%					

	Q	Р	М	То	Tr
Quaternary	211	3	4	0	0
Pliocene	0	15	2	0	0
Messinian	4	7	74	0	0
Tortonian	0	0	0	25	0
Trias	0	0	0	0	25
Commission error	3.21	11.76	12.94	0	3.85
Omission error	2.31	40	7.5	0	0
к=0.905					
Overall accuracy = 94.3%					