

Article



1

2

3

4

5

6 7

8

9

10

11

12

13

14

Conservation strategy for palm groves: Optimal chemical control model for Red Palm Weevil

Y. Solano-Rojas¹, M. Gámez¹, I. López^{2*}, J. Garay³, Z. Varga⁴ and T. Cabello¹

- ¹ Center for Agribusiness Biotechnology Research, University of Almería, La Cañada de S. Urbano, s/n, Almería, 04120, Spain; <u>ysr376@inlumine.ual.es</u> (Y.S.R.); <u>mgamez@ual.es</u> (M.G.), <u>tcabello@ual.es</u> (T.C.)
 - Department of Mathematics, University of Almería, La Cañada de San Urbano, 04120, Almería, Spain; milopez@ual.es
- ³ Centre for Ecological Research, Institute of Evolution, and MTA-ELTE Theoretical Biology and Evolutionary Ecology Research Group and Department of Plant Systematics, Ecology and Theoretical Biology, L. Eötvös University, Budapest, Hungary; garayj@ttk.elte.hu
- ⁴ Department of Mathematics and Modelling, Institute of Mathematics and Basic Science, Hungarian University of Agriculture and Life Sciences, Gödöllő, Hungary; <u>Varga.Zoltan@uni-mate.hu</u>
- * Correspondence: <u>milopez@ual.es</u>

Abstract: In the Mediterranean area, a major concern is the conservation of palm tree landscapes 15 against the red palm weevil, Rhynchophorus ferrugineus (Olivier, 1790). The methodological approach 16 of conservation ecology, such as multidisciplinary modelling also applies in the management of 17 cultural landscapes concerning ornamental plants like palm trees of the area. In the paper we pro-18 pose a dynamic model for the control of the red palm weevil, contributing in this way to the sus-19 tainability of an existing cultural landscape. The primary data set collected is a sample from the 20 density-time function of a two-cohort pest population. This data set suggests a bimodal analytic 21 description. If, from this data set, we calculate a sample from the accumulated density-time function 22 (the integral of the density-time function), it displays a double sigmoid function (with two inflec-23 tions). A good candidate for the analytical description of the latter is the sum of two logistic func-24 tions. As for the dynamic description of the process, a two-dimensional system of differential equa-25 tions can be derived, where the solution's second component provides the analytical description of 26 the original density-time function for the two-cohort population. Since the two cohort waves appear 27 in all three cycle stages, this reasoning applies to the subpopulations of larvae, pupae, and adults. 28 The model fitting is always performed using the SimFit package. Based on these dynamics, an op-29 timal chemical control model is also suggested as a plant conservation tool. 30

Keywords: insect population dynamics; cultural landscape; plant protection; Rhynchophorus ferrugi-31neus; numerical modelling; sigmoid functions32

33

34

1. Introduction

The red palm weevil, *Rhynchophorus ferrugineus*, hereinafter referred to as RPW, 35 (Olivier, 1790) (Col.: Dryophthoridae), is a species native to Asia and Polynesia, and is 36 characterized as an invasive pest of great severity and economic importance worldwide 37 [1,2]. This species has expanded from its area of origin to different continents. It has been 38 recorded in 28 countries in Asia, 6 in Africa, 1 in North America, 2 in Central America and 39 the Caribbean, 14 in Europe, and 5 in Oceania, causing serious problems in coconut trees, 40 both in crop cultivation and in ornamental use [1,3].

In Spain, RPW has spread widely over the Mediterranean coast, the interior of the peninsula and the islands, causing significant ecological and economic damage in areas such as the "Palmeral de Elche" (in the Valencian Community), declared a World Heritage Site by UNESCO, and in the *Phoenix canariensis* forest on the Canary Islands, which is a

Citation: Solano-Rojas, F.; Gámez, M.; López, I.M Garay, Z.; Varga, Z.; Cabello, T. Conservation strategy for palm groves: Optimal chemical control model for red palm weevil . *Agronomy* 2021, *11*, x. https://doi.org/10.3390/xxxx

Academic Editor: Firstname Lastname

Received: date Accepted: date Published: date

Publisher's Note: MDPI stays neutral with regard to jurisdictional claims in published maps and institutional affiliations.



Copyright: © 2021 by the authors. Submitted for possible open access publication under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses /by/4.0/). natural heritage site and represents the most relevant source of genetic variation for this 46 palm tree [1,4,5]. 47

The damage caused by *R. ferrugineus* has a social, cultural and economic impact on 48 the production systems and ecosystems in which the various palm species are grown 49 and/or protected, since it affects the production of food, ornamental material and renew-50 able energy, as well as ecological bioremediation services, airflow regulation in urban en-51 vironments and biodiversity conservation, among others [6-8]. In Spain during the 2005– 52 2009 period, between 47,000-50,000 infested palm trees were destroyed; this involved con-53 tainment/eradication costs of 44.5 million euros, particularly in the Valencian Community 54 where professional and family-managed nurseries were affected [9,6,10]. In this regard, 55 the FCEC [6] considered that infested (but not destroyed) palm trees might result in losses 56 of between 96 and 288 million euros. 57

The severity of *R. ferrugineus* and the problems associated with its control, including 58 the difficulty of detecting infested palm trees early, the risk of mass captures in non-in-59 fested areas and the loss of control strategy effectiveness [7], motivate the search for new 60 tools that increase the bio-ecological knowledge for dealing with RPW populations. In this 61 regard, mathematical models can offer a holistic approach to understanding the biological 62 behaviour of species, and they are an instrument for predicting and/or simulating com-63 plex systems that include the population dynamics of the pest and its control strategies 64 [11-13]. 65

In the Plant Protection field, mathematical models have focused on using sigmoid functions such as Verhulst-Pearl or logistics, Gompertz, Weibull, Richards and monomolecular, as well as those models that combine them [14-17]. These functions have also been integrated to optimize the use of the resources and time spent on combating pests, through the formulation of optimal control problems aimed at keeping a pest population below the economic damage level as well as to reduce the need to implement control strategies [11,12,18,13,19].

The existing literature on mathematical models related to ecological aspects of R. fer-73 rugineus is scarce, with only the work of Rossini et al. [20], who proposed a linear model 74 for RPW development as a function of temperature. However, Hansen et al. [21] adapted 75 a logistic model for another curculionidae species, Dendroctonus rufipennis (Kirby), based 76 on temperature as a diapause prediction factor of the insect's fourth larval stage. It should 77 be noted that the larval diapause in curculionidae has also been recorded for Curculio ele-78 phas Gyllenhal, C. sikkimensis (Heller) and Smicronyx fulvus LeConte, where the larvae 79 were subjected to temperatures below 15 °C [22-25]. 80

In the *R. ferrugineus* larvae, Martín & Cabello [1] recorded a slowdown in the development of their last stages when the temperature dropped and remained in the 10 - 15 °C range for a period of more than 80 days, arguing that this phenomenon was due to a larval diapause, because the delay in the larval development and metabolic activity was related to changes in temperature [26,27].

The importance of RPW within palm production systems and/or ecosystems, and the need to deepen our understanding of the population behaviour of its stages is fundamental to the development of mathematical models that can describe the population dynamics of the larvae, pupae, and adults of *R. ferrugineus*, and to propose an optimal solution to control their larvae. This has been the objective of this work. 90

The resulting modelling-methodological development also contributes to the sustainable management of the involved cultural landscape of palm groves and ornamental palm trees. 93

2. Materials and Methods

2.1. Biological data used

Biological data on the development of the developmental stages, such as on the longevity of *R. ferrugineus* adults, were obtained from a trial carried out in the 'Cortijo del 97

94

Olivar' (Almuñecar, Granada, Spain; 36.748259N, 3.689860S) [1]. This was performed under field conditions and using sugar cane as a feeding substrate for the larvae and adults. 99

2.2. Mathematical model

The primary data set collected is a sample from the density-time function of a twocohort pest population. This data set suggests a bimodal analytic description.

Originally, the single logistic function:

 $\frac{K}{1 + \left(\frac{K}{x_0} - 1\right)e^{-rt}}$ (1) 104

is the solution of the logistic differential equation:

$$t' = rx\left(1 - \frac{x}{K}\right) \tag{106}$$

with the initial condition $x(0) = x_0$. Function (1) is sigmoid, its derivative, with appropriate constants $a_0, a_1, a_2 > 0$ is 108

J

$$\nu_1(t) = \frac{a_0 e^{-a_1 t}}{\left(1 + a_2 e^{-a_1 t}\right)^{2'}}$$
(2) 109

displaying a unimodal curve. The sample from the density-time function of a two-cohort 110 pest population suggests a bimodal analytic description, and for that, the sum of two functions of type (2) is a promising candidate [15]: 112

$$y_2(t) = \frac{a_0 e^{-a_1 t}}{\left(1 + a_2 e^{-a_1 t}\right)^2} + \frac{a_3 e^{-a_4 t}}{\left(1 + a_5 e^{-a_4 t}\right)^2},$$
(3) 113

where $a_0, a_1, a_2, a_3, a_4, a_5 > 0$ are the fitting parameters.

If we calculate a sample from the *accumulated density-time function* (the integral of the density-time function) from the data set of the density-time function, it shows a double sigmoid function (with two inflections). From the above, we conclude that a good candidate for the analytic description of the latter is the sum of two logistic functions (1): 118

$$\frac{K_1}{1 + \left(\frac{K_1}{x_{01}} - 1\right)e^{-r_1t}} + \frac{K_2}{1 + \left(\frac{K_2}{x_{02}} - 1\right)e^{-r_2t}}.$$
(4) 119
(2) are the fitting parameters.

Here, K_i , r_i , $x_{0i} > 0$ (*i*=1,2) are the fitting parameters.

It is worth emphasizing that, if we consider a two-cohort pest population of *Rhyn-* 121 *chophorus*, the above reasoning can be applied to all the developmental stages: the larvae, 122 pupae, and adults. 123

2.3. Dynamic model of optimal chemical control

Considering any given stage, from functions (2) and (3) we easily obtain the following system of differential equations, where y_1 is the density-time function of a single cohort, and y_2 is the density-time function of the two-cohort population: 127

$$y_1' = a_1 y_1 \left(1 - \frac{2}{1 + a_2 e^{-a_1 t}} \right)$$
(5) 128

$$y_2' = a_1 y_1 \left(1 - \frac{2}{1 + a_2 e^{-a_1 t}} \right) + a_4 (y_2 - y_1) \left(1 - \frac{2}{1 + a_5 e^{-a_4 t}} \right).$$
(6) 129

Although the dynamic model (5)-(6) can be adapted to any stage, for the chemical 130 control of *Rhynchophorus*, system (5)-(6) will be used for a two-cohort larval population 131 [1]. Let us fix a operational time interval [0,T] and define the set of admissible controls $U_{\varepsilon}[0,T]$ consisting of piece-wise constant functions over a fixed uniform division of interval [0,T] with $0 \le u(t) \le \varepsilon$. Let constants μ_1 , $\mu_2 > 0$ express the efficiency of the 134 chemical on the respective populations. Then, from the (5)-(6) dynamics, we obtain the 135 following control system: 136

$$y_1' = a_1 y_1 \left(1 - \frac{2}{1 + a_2 e^{-a_1 t}} \right) - \mu_1 u y_1 \tag{7}$$

$$y_2' = a_1 y_1 \left(1 - \frac{2}{1 + a_2 e^{-a_1 t}} \right) - \mu_1 u y_1 + a_4 (y_2 - y_1) \left(1 - \frac{2}{1 + a_5 e^{-a_4 t}} \right) - \mu_2 u y_2$$
(8) 138

Now, on the basis of this control system, we set up the following optimal control 140 problem: suppose that the damage caused by larval density y_2 in unit time is αy_2 , then 141 the total damage during the time interval [0,T] is $\int_0^T \alpha y_2(t) dt$. If this damage is to remain 142

100

103

105

114

124

below a boundary, H, for the palm tree to survive, and we wish to minimize the cost of 143 the chemical control proportional to $\int_0^T u(t) dt$, we obtain the following constrained opti-144 mal control problem: 145

$$\Psi(u) = \int_{0}^{T} u(t)dt \to min,
 u \in U_{\varepsilon}[0, T]
equations (5) - (6)hold
\int_{0}^{T} \alpha y_{2}(t)dt \leq H$$
(9) 146

 $y_1(0), y_1(0)$ are given.

. .

2.4. Software used

148

151

156

161

164

147

The above-mentioned mathematical models have been fitted to the data using the 149 TableCurve 2d v 5.0 [28] and SimFit v 6.9.8 [29] software packages. 150

3. Results

The results found were used to carry out the adjustment to the proposed mathemat-152 ical model that explains the population dynamic of the insect's life-cycle stages (Section 153 3.1). Subsequently, with this model, a control variable was used that would allow us to 154 set the time for the chemical control of the pest in order to obtain an optimal result. 155

3.1. Results of model fitting

The results show that a portion of the larval population of *R. ferrugineus* developed 157 normally (relative maximum in tp1), while another portion of the population lengthened 158 its development up to 370 days (Figure 1). In the pupal and adult stages, two relative 159 maxima (tp1 and tp3) are shown with a distance between them of approximately 160 days. 160

Table 1. Values of fitting parameters of model (3) for the all stages of pest population of 162 Rhynchophorus 163

Stage			Statistical parmeters						
	a_0	a_1	<i>a</i> ₂	<i>a</i> ₃	<i>a</i> ₄	<i>a</i> ₅	d.f	R^2	Р
Larvae	673.739	0.04410	3.56691	2117.26	0.01967	80.0043	38	0.97654	< 0.01
Pupa	74980.4	0.05752	792.265	10500.9	0.02003	115.495	40	0.97744	< 0.01
Adult	28372.7	0.04231	485.713	218719	0.02546	2901.76	40	0.95999	< 0.01



Figure 1. Fitted curve of density-time function model (3) for larvae (a), pupae (b) and adults (c) of *Rhynchophorus ferrugineus*.

We note that the R^2 value indicates that the goodness of fit is better (higher) for the double logistic function fitted to the accumulated data (0.99951) than for the fitting dynamics (5)-(6) (0.90319). Similar results were obtained for the rest of the analysed data. This observation justifies the use of a sigmoid function fitted to the accumulated data, 169 smoother than the original density data, which displayed more random oscillations. 170

Subsequently, double logistic curves have also been fitted to the accumulated density 171 data (see Table 2 and Figure 2). In the latter, we also indicate the time moments t_k , where 172 the minima and maxima of the densities are attained, according to the inflexions of the accumulated densities. 174

Stage	Term (i)	Fitti	ng Param	Statistical Parameters			
Buge	1 ci iii (<i>i</i>)	Ki	χ_{0i}	r i	d.f.	R^2	Р
Larvae	1	2951.43	214.53	0.06771	37	0.99764	< 0.01
	2	1673.39	57.6115	0.01661			
Pupa	1	1810.51	4.8024	0.05484	40	0.99872	< 0.01
	2	4621.58	47.1067	0.01889			
Adult	1	1342.24	1.2492	0.04789	43	0.99951	< 0.01
	2	3031.58	1.32482	0.02461	- 10		

Table 2. Values of fitting parameters of double logistic functions for pest populations of
 176

 Rhynchophorus. 177



178 179

175

6 of 11



Figure 2. Mathematical models (double logistic functions) fitted to the accumulated data of the palm pest species, *Rhynchophorus ferrugineus* (a) larvae,

(b) pupae and (c) adults stages), also displaying the corresponding bimodal density time functions.

3.2. Solution of the optimal control problem

For a palm tree to survive, our objective is to keep the effect of the larval population 181 under a boundary, H, at minimum cost. Using the Table 1 fitting parameters, we solved 182 the optimal control problem (9) with H = 2000 units of biomass, T=450, $\mu_1 = 0.95$, $\mu_2 = 0.5$ 183 $\alpha = 0.7, \varepsilon = 0.1, y_1(0) = 13 y_2(0)=14.$ 184

We solved the optimal control problem applying the toolbox developed for MatLab 185 186

55 50 n n Without Control 45 40 3 State Variables 0.03 30 25 0.04 With Control 20 0.03 1 0.02 10 0.0 0 L 0 50 100 150 300 350 450 200 250 400 Time Tim (b) (a)

Figure 3. (a) Trajectories for larva stage y_2 without control in model (5)-(6), and with optimal control. (b) Optimal control to be applied, solution of problem (7)-(8).

4. Discussion

A Plasticity is well understood when it takes the form of responding to predictive 189 environmental signals received during the individual's lifespan. However, the so-called 190 mixture of intragenotypic strategies has been neglected, perhaps due to the general as-191 sumption that it must be non-adaptive [31]. In this regard, several species of insects, espe-192 cially from the Coleoptera order, may present two types of larval diapause (simple or 193 prolonged), leading to diverse cohorts that differ in their life cycles, especially in terms of 194 duration. The causes of what Ushatinskyaya [32] called "superdiapause" are poorly stud-195 ied and not understood in detail. In our case, it seems clear from the results that RPW 196 belongs to this group of insects. 197

The results for the first species, *R. ferrugineus*, showed that a portion of the larval 198 population develop normally, but another portion could lengthen their development up 199 to 370 days (Figure 1); this is demonstrated by the two relative maxima found in the pupal 200 and adult stages. The above statement might indicate that the diapause exists as a survival 201 mechanism. This phenomenon was later verified in other trials [1]. The presence or lack 202 of a diapause in this species is crucial for the early detection and control of the pest, as 203 well as for border inspections, since detection is carried out by ultrasound - if the larvae 204 are in diapause, they are not feeding, and therefore will not make a noise with their jaws 205 that can be detected [33]. Likewise, the results can be used to develop more complex pre-206 dictive models to track the dynamics and expansion of this pest species. 207

The results of the logistic developed for the population dynamics of the RPW larvae 208 shows an elongation of larval development that would relate to the diapause manifesting 209 as a survival mechanism. Martín & Cabello [1] noted that the diapause of RPW larvae was 210 stimulated by a decline in temperature, of values between 10 °C and 15 °C, during the 211

by Banga et al. [30], the result of which are shown in Figure 3.

180

187

larval growth stage. Additionally, they indicated that this phenomenon promoted the division of the larval population into two groups: the first formed before the temperature drop occurred, in which the larvae continued their normal development (such as that recorded in tp₁, Figure 1a), while the second group delayed its development by 170 days (similar to that shown from tp₂ onwards, Figure 1a), with the consequent delay in pupal and adult morphogenesis (as in the relative maxima, tp₁ and tp₃, in Figures 1b and 1c, respectively).

The larval behaviour of *R. ferrugineus* may represent a survival strategy that offers 219 the maximum development opportunity in a univoltine cycle, as one group of larvae is 220 able to accelerate their development to promote adult formation during the spring, while 221 the other can slow down its development, influenced by the low winter temperatures, 222 allowing adults to form that emerge during the autumn. This behaviour has also been 223 recorded by Hansen et al. [21] for the curculionid D. rufipennis, whose larval diapause was 224 mathematically modelled in a logistic function that considers the thermal threshold as a 225 predicting factor. Other curculionidae may also have a larval diapause in response to the 226 drop in temperature, as is the case with Curculio elephas Gyllenhal [22,23], C. sikkimensis 227 (Heller) [24] and Smicronyx fulvus LeConte [25]. 228

Whether or not the RPW larvae are in diapause is crucial for early detection and pest control because most RPW inspection systems include equipment capable of detecting ultrasound produced by the larvae during feeding [34, 35]. Therefore, detecting no noise will not mean the absence of larvae inside the palm stems, since diapause larvae do not feed [33]. 233

The mathematical models developed for the larval, pupal, and adult stages of RPW 234 constitute a valuable tool for bio-ecological and/ or prediction studies of the population 235 level of this pest in various Spanish zones where the ambient temperature varies over the 236 year, and can even stay below 15 °C during the winter months. At this time, the larvae can 237 slow their development as a survival mechanism, as recorded by Martín & Cabello [1] in 238 the municipality of Almuñecar (Granada, Spain) during the months from November to 239 March, in which the temperature, both of the air and inside the palm tree, remained be-240 tween 10 °C and 15 °C, with fluctuations within the palm tree of around 10 °C for more 241 than 80 days. 242

In this regard, mathematical models can be used in various parts of Spain where palm 243 trees are grown, such as the Andalusian coastal zones of the Mediterranean and the coastline from the Ebro Delta to Gibraltar, the *Valle bajo* of the Guadalquivir and Guadiana, as well as in coastal areas of the *Rias Bajas* in Galicia, where the ambient temperature can range from 10 °C to 12.5 °C during the month of January [36], also having an impact on the internal temperature of the palm trees. 248

Moreover, the optimal control model for RPW larvae reveals that the application of a chemical control measure can significantly reduce the initial larval population peak over the first 50 days. The action of chemical control also produces a significant decline in the second larval maximum, which begins to form from about day 100 in the uncontrolled population. 253

In turn, the rise in the chemical control trajectory seen in Figure 4, which begins after day 100, corresponds to the need to increase the use of insecticide to keep the palm biomass threshold below the economic damage level, since the larval development continues in this period, having been delayed by the temperature decline experienced by the population without chemical control. Likewise, this increase in the control trajectory can be related to the formation of RPW pupae and/or adults, which require greater control. 259

The logistic models developed for the population dynamics of the *R. ferrugineus* 260 stages, as well as the optimal control model proposed, are instruments that can be incorporated into integrated pest control programmes, with the aim of improving decisionmaking and reducing the cost of managing the RPW population. Similarly, these tools can be included within more complex prediction models, allowing us to understand RPW dynamics and expansion. 260

271

276

277

278

281 282

285

292

293

294

295

296

297

302 303

304

305

In summary, the results from the logistic models, for the pest species as well as for the different aspects of their biology/ecology, suggest that they could be an excellent tool to use in Integrated Pest Management (IPM) programmes. This may also corroborate the results found regarding the dynamics of crop diseases [14,15], as their use can be generalized to Crop Protection. 270

Author Contributions: Conceptualization, T.C., Y.S.R. and J.G.; Methodology and formal analysis:272T.C., Y.S.R., Z.V. M.G., I.L. and J.G.; Software, M.G. and I.L.; Visualization, I.L. and T.C.; Writing –273original draft: J.G., Z.V., Y.S.R., I.L., M.G., and T.C. All authors have read and agreed to the present274version of the manuscript.275

Funding: The research was funded by the Fundación Carolina.

Data Availability Statement: Not applicable.

Acknowledgments: I.L. also thanks the support from CDTIME (University of Almería).

Conflicts of Interest: The authors declare no conflict of interest. The sponsors had no role in the 279 design, execution, interpretation, or writing of the study. 280

References

- Martin, M.M.; Cabello, T., 2005. Biología y ecología del Curculiónido rojo de la palmera, *Rhynchophorus ferrugineus* (Olivier, 283 1790) (Col.: Dryophthoridae). Universidad de Almeria. Almeria, Spain, 2008; 202 pp. 284
- 2. Cabello, T. Rhynchophorus ferrugineus: biología, dispersión y modo de acción. Phytoma 2012, 235, 36 38.
- CABI, 2013. Invasive species compendium: *Rhynchophorus ferrugineus*. (Last modified: 25 November 2019) [286 <u>https://www.cabi.org/isc/datasheet/47472</u>]
- Ferry, M.; Gómez, S. El picudo rojo de la palmera datilera: gravedad de la plaga en España y necesidad de un cambio radical y urgente de estrategia en la lucha. *Phytoma* 2007, 184, 1-4.
 289
- Cobos, J.M. Situation of *R. ferrugineus* in Spain. Red palm weevil control strategy for Europe: International Conference. Valencia, 290 Spain, 2010, 5-6 May.
- FCEC (Food Chain Evaluation Consortium). 2011. Quantification of costs and benefits of amendments to the EU plant health regime: Final report. Disponible en: <u>https://ec.europa.eu/food/sites/food/files/plant/docs/ph biosec rules fcec final report economic study plant health en.pdf</u> Consultado 09-11-2020
- 7. Giblin-Davis, R.M.; Romeno Faleiro, J.; Jacas, J.A.; Peña, J.E.; Vidyasagar, P.S.P.V. 2013. Biology and management of the red palm weevil, *Rhynchophorus ferrugineus*. In: Peña JE. (Eds.), Potential invasive pests of agricultural crops. Pp.
- 8. Soroker, V.; Colazza, S. Handbook of major palm pests: biology and management. Wiley Blackwell P. 2017.
- Suárez, J.M.C. Situation of *R. ferrugineus* in Spain. Red palm weevil Control Strategy for Europe: International Conference. 298 Valencia, Spain, 2010, May 5 – 6. 299
- Jacas, J.A.; Dembilio, O.; Llácer, E. Research activities focused on management of red palm weevil at the UJI-IVIA Associated Unit (Region of Valencia, Spain). OEPP/EPPO Bulletin, 2011, 41, 122 – 127.
 301
- 11. Rafikov, M.; Balthazar, J.M. Optimal pest control problem in population dynamics. *Computational & Applied Mathematics* **2005**, 24(1), 65 81.
- 12. Meng, X.; Song, Z.; Chen, L. A new mathematical model for optimal control strategies of integrated pest management. *Journal* of *Biological Systems* **2007**, 15(2), 219 234.
- Dabbs, K. Optimal control in discrete pest control models. University of Tennessee Honors Thesis Projects. 2010. Disponible en: 306 https://trace.tennessee.edu/utk_chanhonoproj/1375
 307
- Amorim, L.; Bergamin-Filho, A; Hau, B. Analysis of progress curves of sugarcane smut on different cultivars using functions of double sigmoid pattern. *Phytopathology* 1993, 83, 933-936.
 309
- Hau, B.; Amorim, L.; Bergamin-Filho, A. Mathematical functions to describe disease progress curves of double sigmoid pattern. 310 Phytopathology 1993, 83, 928-932. 311
- Carreño, R. 1996 Modelos logísticos. Aplicaciones a la Agronomía. Facultad de Ciencias Experimentales. Universidad de Almeria. 1997. PhD dissertation. Almeria, Spain: 168 pp.
 313
- Cabello, T.; Carreño, R. Métodos logísticos aplicados a la fenología de Noctuidos Plagas en el Sur de España (Lep.: Noctuidae).
 Boletin de Sanidad Vegetal Plagas 2002, 28: 319-226.
 315
- Rafikov, M.; Angelelli, T. Optimization of biological pest control of sugarcane borer. 18th IEEE International Conference on Control Applications Part of 2009 IEEE Multi-Conference on Systems and Control Saint Petersburg, Russia, 2009, July 8 – 10.
 317
- Gallego, J.R.; López, I.; Gámez, M.; Cabello, T.; Varga, Z.; Garay, J. Simulation model applied to biological pest control by entomophagous species in commercial tomato greenhouses. *Hung. Agric. Eng.* 2013, 25, 67 – 70.
 319

- Rossini, L.; Severini, M.; Contarini, M.; Speranza, S. Distributed delay models: a proposal of application in urban context to forecast pest insects' life cycle. In: A. Leone & C. Gargiulo (Eds.), Environmental and territorial modelling for planning and design. 2018. Pp. 169-178. Doi: 10.6093/978-88-6887-048-5
 320
- Hansen, E.M.; Bentz, B.J.; Powell, J.A.; Gray, D.R.; Vandygriff, J.C. Prepupal diapause and instar IV developmental rates of the spruce beetle, Dendroctonus rufipennis (Coleoptera: Curculionidae, Scolytinae). *Journal of Insect Physiology* 2011, 57, 1347 – 1357.
- 22. Menu, F. Diapause development in the chestnut weevil Curculio elephas. Entomol. Exp. Appl. 1993, 69, 91 96.
- Menu, F.; Debouzie, D. Larval development variation and adult emergence in the chestnut weevil *Curculio elephans* Gyllenhal (Col., Curculionidae). J. Appl. Ent. 1995, 119, 279 284.
 327
- Higaki, M. Effect of temperature on the termination of prolonged larval diapause in the chestnut weevil *Curculio sikkimensis* 328 (Coleoptera: Curculionidae). *Journal of Insect Physiology* 2005, 51, 1352 – 1358.
- Prasifka, J.R.; Rinehart, J.P.; Yocum, G.D. Nonconstant thermal regimes enhance overwintering success and accelerate diapause development for *Smicronyx fulvus* (Coleoptera: Curculionidae). *Journal of Economic Entomology* 2015, 108(4), 1804 1809.
 331
- Danks, H.V. Insect dormancy: An ecological perspectiva. Biological survey of Canada. Monograph series Nº 1. National Museum of Natural Science. Ottawa, 1987, 439 pp.
 333
- 27. Gordh, G.; Headrick, D.H. A dictionary of entomology. CABI Publishing. Wallingford, 2001, 1032 pp.
- 28. Jandel Scientific. Table Curve 2D-User's manual. Version 5..0. Jandel Scientific. San Rafael, 1994.
- Bardsley, W. G. SIMFIT: Simulation, fitting, statistics and plotting. Reference manual.University of Manchester, Manchester, 336 UK, 2010.
 337
- Banga, J.R.; Balsa-Canto, E.; Moles, C.G.; Alonso, A.A. Dynamic optimization of bioprocesses: Efficient and robust numerical strategies. J. Biotechnol. 2005, 117, 407–419.
 339
- Menu, F.; Debouzie, D. Coin-flipping plasticity and prolonged diapause in insects: example of the chestnut weevil Curculio elephas (Col.: Curculionidae). *Oecologia* 1993, 93, 367-373.
 341
- 32. Ushatinskaya, RS. A critical review of the superdiapause in insects. Ann Zool 1984, 21, 3-30.
- Cabello, T. Population biology and dynamics of the Red Palm Weeevil, *Rhynchophorus ferrugineus* (Olivier, 1790) (Coleoptera: 343 Dryophothoridae) in Spain. I Jornada Internacional sobre el Picudo Rojo de las Palmeras. Fundación Agrolimed, Generalitat Valenciana. Valencia, Spain, 2006, 19-34.
- Potamitis, I.; Ganchev, T.; Kontodimas, D. On automatic bioacoustic detection of pests: The cases of Rhynchophorus ferrugineus and Sitophilus oryzae. *Journal of Economic Entomology* 2009, 102(4), 1681 – 1690.
 347
- Gutiérrez, A.; Ruiz, V.; Moltó, E.; Tapia, G.; Téllez, M.M. Development of a bioacoustic sensor for the early detection of Red Palm Weevil (*Rhynchophorus ferrugineus* Oliver). Crop Protection 2010, 29, 671 – 676.
 349
- 36. Centro Nacional de Información Geográfica. Instituto Geográfico Nacional. Atlas Nacional de España. Available in: <u>http://cen-</u> 350 trodedescargas.cnig.es/CentroDescargas/busquedaRedirigida.do?ruta=PUBLICACION_CNIG_DATOS_VARIOS/aneTematico/Espana_Temperatura-media-de-las-maximas-de-enero_1981-2010_mapa_14670_spa.pdf# Last access: 11-11-2020 352

325

334

335