Efficient query processing on large spatial databases A performance study

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Abstract

Processing of spatial queries has been studied extensively in the literature. In most cases, it is accomplished by indexing spatial data using spatial access methods. Spatial indexes, such as those based on the Quadtree, are important in spatial databases for efficient execution of queries involving spatial constraints and objects. In this paper, we study a recent balanced disk-based index structure for point data, called xBR+-tree, that belongs to the Quadtree family and hierarchically decomposes space in a regular manner. For the most common spatial queries, like *Point Location*, *Window*, *Distance Range*, *Nearest Neighbor* and *Distance-based Join*, the R-tree family is a very popular choice of spatial index, due to its excellent query performance. For this reason, we compare the performance of the xBR+-tree with respect to the R*-tree and the R+-tree for tree building and processing the most studied spatial queries. To perform this comparison, we utilize existing algorithms and present new ones. We demonstrate through extensive experimental performance results (I/O efficiency and execution time), based on medium and large real and synthetic datasets, that the xBR+-tree is a big winner in execution time in all cases and a winner in I/O in most cases.

Keywords: Spatial Databases, Spatial Access Methods, Quadtrees, xBR-trees, R-trees, Query Processing, Performance Evaluation

1. Introduction

Due to the demanding need for efficient spatial access methods in many spatial database applications [1, 2], significant research effort has been devoted to the development of new spatial index structures [3, 4, 5]. However, as shown in several previous comparative studies [6, 7, 8, 9], there is no unique index structure that works efficiently, in all cases. These performance studies were executed taking into account a great variety of modern applications, where a variety of Spatial Queries arise.

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The most common spatial queries where points are involved are Point Location, Window, Distance Range, Nearest Neighbor and Distance-based Join Queries. Moreover, such queries have been also used as the basis of many complex operations in advanced applications (e.g. multimedia databases [10], medical images databases [11], geometric databases [12], CAD [13], Geographical Information Systems (GIS) [14], etc).

Hierarchical index structures are useful because of their ability to focus on the interesting subsets of data [3, 4]. This focusing results in an efficient representation and improved execution times on query processing and is, thus, particularly useful for performing spatial operations [5]. Important advantages of these structures

are their conceptual clarity and their great capability for query processing. The Quadtree is a well known hierarchical index structure, which has been applied successfully on GIS, image processing, spatial information analysis, computer graphics, digital databases, etc. [14, 5]. It was introduced in the early 1970s [15], it is based on the principle of recursive decomposition of space and has become an important access method for spatial data [16].

The External Balanced Regular (xBR)-tree [17] is a secondary memory structure that belongs to the Quadtree family (widely used in GIS applications [14]), which is suitable for storing and indexing multidimensional points (and, in extended versions, line segments, or other spatial objects). We utilize an improved version of xBR-tree, called xBR+-tree [18], which is also a disk-resident structure. The xBR+-tree improves the xBR-tree in the node structure and in the splitting process. The node structure of the xBR+-tree stores information which makes query processing more efficient.

In this paper, we compare the xBR⁺-tree with popular R-tree indexes, regarding storage requirements, time needed for the tree construction and spatial query performances. The family of R-trees has been populated with lots of assorted variations. Each variation tries to optimize a particular aspect (splitting, deletion, etc). However, we concentrate on the R*-tree [19], because *it is the most commonly employed spatial indexing structure in the spatial database community* [4, 2], and to the R⁺-tree, because *it is an index structure based on disjoint decomposition of space like the xBR⁺-tree.*

This paper substantially extends our previous work [20] (where xBR-trees were compared to R*-trees using single dataset queries and datasets of medium size and it was shown that the two structures are comparable) and [18] (where a new tree, the xBR+-tree, was presented and compared to the xBR-tree using single dataset queries and datasets of medium size and it was shown that the two structures are comparable in building, while the xBR+-tree is a winner in query processing) and its contributions include the following:

- The presentation of a new alternative Depth-First (DF) algorithm for Distance Range Queries (*DRQs*), *K* Nearest Neighbor Queries (*KNNQs*) and Constrained *K* Nearest Neighbor Queries (*CKNNQs*), utilizing a minimum binary heap (*minHeap*) instead of sorting on the xBR⁺-tree, R*-tree and R⁺-tree.
- The presentation of the first algorithms for K Closest Pair Queries (KCPQs), εDistance Join Queries (εDJQs) on the xBR⁺-tree, and presentation of

- new alternative DF algorithms for KCPQs and $\varepsilon DJQs$, utilizing a minHeap instead of sorting, on R*-trees and R⁺-trees,
- A detailed performance comparison (I/O and execution time) of xBR⁺-trees (non-overlapping trees of the quadtree family) against R⁺-trees (non-overlapping trees of the R-tree family) and R*-trees (industry standard belonging to the R-tree family) on tree building, single dataset queries (Point Location Queries -PLQs-, Window Queries -WQs-, DRQs, KNNQs and CKNNQs) and dual dataset (distance-based join) queries (KCPQs, εDJQs). Note that the performance study was conducted on medium and large spatial (real and synthetic) datasets.

Note that, in this paper we utilize large spatial datasets (where the quantifier "large" designates several tens of millions of spatial objects) since we believe that such datasets can be effectively processed in centralized systems, if efficient methods are used. Even larger (huge) datasets would require the utilization of methods on parallel and distibuted environments (e.g. http://spatialhadoop.cs.umn.edu).

This paper is organized as follows. In Section 2 we review related work on comparing spatial access methods, regarding spatial query processing and provide the motivation for this work. In Section 3, we briefly review the main characteristics of the R-trees (highlighting the R*-tree and R*-tree). In Section 4, we describe the xBR*-tree. In Section 5, we present the algorithms for processing spatial queries, where one or two datasets are involved, over R-trees and the xBR*-tree. In Section 6, we show results of the extensive experimentation performed, using real and synthetic datasets, for comparing the performance of the two R-trees index structures (R*-tree and R*-tree) and the xBR*-tree. Finally, in Section 7 we provide the conclusions arising from this research work and discuss related future work directions.

2. Related Work and Motivation

The Quadtree belongs to a class of hierarchical data structures whose common property is that they are based on the principle of *recursive regular decomposition of space*. These structures are characterized as *space-driven access methods* according to [1]. It is most often used to partition a 2d space by recursively subdividing it into four quadrants or regions: NW (North West), NE (North East), SW (South West) and SE (South East). According to [21], Quadtrees can be classified by following three principles: (1) the type of data

that they are used to represent (points, regions, curves, surfaces and volumes), (2) the principle guiding the decomposition process, and (3) the resolution (variable or not).

In order to represent Quadtrees, there are two approaches: the pointer-based and pointerless approaches. In general, the pointer-based Quadtree representation is one of the most natural ways to represent a Quadtree structure. In this method, every node of the Quadtree will be represented as a record with pointers to its four sons. Sometimes, in order to process specific operations, an extra pointer from a node to its father could also be included. The xBR⁺-tree belongs to the category of pointer-based Quadtrees. On the other 190 hand, the pointerless representation of a Quadtree defines each node of the tree as a unique locational code [14]. By using the regular subdivision of space, it is possible to compute the locational code of each node in the tree. The linear Quadtree is an example of pointerless Quadtree. We refer the reader to [14, 3, 5, 22] for further details.

The xBR⁺-tree [18] belongs to the category of pointer-based Quadtrees and it is an extension of the xBR-tree [17, 20]. The xBR⁺-tree has similarities 200 with other well-known multidimensional access methods [16]. For example, the form of nodes in xBR⁺-trees has similarities to the form of nodes of Generalized BDtrees (GBD-trees) [23]. GBD-trees are based on kdtree-like decomposition of space, while xBR+-trees on 205 Quadtree-like decomposition. Moreover, the splitting of internal nodes in xBR+-trees is handled in a more sophisticated way than in GBD-trees. The xBR+-tree has also similarities to the hB-tree [24], where space is also partitioned according to kd-trees (unlike the xBR⁺- 210 tree, where partitioning follows the data space hierarchy principle) and holey brick-like regions are created. Unlike the hB-tree, in the xBR+-tree, each internal node has only one pointer to a child node and the entries of an internal node are region-pointer pairs and not tree structures (kd-trees), as in the hB-tree. Finally, we refer the reader to [14, 3, 16, 5, 22] for further details on multidimensional access methods.

Regarding the performance comparison of spatial query algorithms using the most cited spatial access methods (R-trees and Quadtrees), several previous research efforts have been published. In [6] a qualitative comparative study was performed taking into account three popular spatial indexes (R*-tree [19], R+-tree [25] and PMR Quadtree [26]), in the context of processing spatial queries (point query, nearest line segment, window query, etc.) in large line segment databases. The conclusion reached was that the R+-tree and PMR

Quadtree were the best when the operations involve search, since they result in a disjoint decomposition of space. On the other hand, the R*-tree was more compact than the R+-tree (and the PMR Quadtree) but its performance was not as good as the R+-tree, due to the non-disjointness of the decomposition induced by it.

In [7], various R-tree variants (R-tree [27], R*-tree and R+-tree) and the PMR Quadtree have been compared for the traditional spatial *overlap join* operation. They showed that the R+-tree and PMR Quadtree outperform the R-tree and R*-tree using 2d GIS spatial data. That is, with respect to the overlap join, the spatial data structures based on a disjoint decomposition of space (like the R+-tree and PMR Quadtree) outperformed spatial data structures based on a non-disjoint decomposition such as the numerous variants of the Rtree including the R*-tree. Moreover, as the size of the output of the spatial join increases with respect to the larger of the two inputs, methods based on a disjoint regular decomposition (like the PMR Quadtree) performed significantly better. Due to the good performance results of the R⁺-tree for overlap join, in this research work, we have compared this structure to the xBR⁺-tree for spatial queries.

Another interesting comparison was presented in [9], where the R-tree and the Quadtree have been contrasted in the context of Oracle Spatial, using a variety of range and Nearest Neighbor (NN) queries on spatial data arising in 2d Geographical Information Systems (GISs). It was shown that, in general, the R-tree outperforms the Quadtree. From this experimental comparison, Oracle, in general, recommends using R-trees over Quadtrees, due to higher tiling levels in the Quadtree that cause very expensive preprocessing and storage costs.

In [28], the R*-tree and a Quadtree index enhanced with Minimum Bounding Rectangle (MBR) keys for the internal nodes (MBRQuadtree) have been compared with respect to the All-Nearest Neighbor (ANN) query. The ANN query takes as input two datasets of multi-dimensional points and computes for each point in the first dataset the NN in the second one. Experimentally, the authors showed that for ANN queries, the MBRQuadtree is a much more efficient indexing structure than the R*-tree index.

In [8], the authors have compared the performance of R-trees and Quadtrees index structures for evaluating the *K*NN and the *K* Distance Join (using the algorithms described in [29]) query operations and the index construction methods (dynamic insertion for the R*tree and bucket Quadtree) and bulk-loading algorithm (Sort-Tile-Recursive, STR, for the R-tree [30] and bulk-loading for the Quadtree). It was shown that the query

processing performance of the R*-tree was significantly affected by the index construction methods, while the Quadtree was relatively less affected by the index construction method. The regular and disjoint partitioning method used by the Quadtree has an inherent structural 285 advantage over the R*-tree in performing KNN and K Distance Join queries. The Quadtree-based index structure could be a better choice than the widely used R*tree for spatial queries when indices are constructed dynamically. Moreover, it was shown that when data are 290 static (i.e. when a bulk-loading algorithm is used for an index construction) and KNNOs / K Distance Join Queries are executed, the STR built R-tree showed the best performance. However, when data are dynamic (i.e. there are frequent updates), a bucket Quadtree be- 295 gins to outperform the R*-tree. This is due to overlap among MBRs that increases with increasing dataset sizes (once the dynamic R*-tree algorithm is used), and the R*-tree performance is degraded.

In the context of performance studies, in [31], an interesting performance comparison (with respect to number of disk read accesses, response time and memory requirements) of distance-based query (Distance Range, K-Nearest Neighbors, K-Closest Pairs and ε Distance Join) algorithms (Depth-First Search -DFS-, Best-First Search -BFS- and Recursive Best-First Search -RBFS-) on R*-trees was presented. The main conclusion was that BFS was the best for all studied distance-based queries, but it may consume many main memory resources. DFS was slightly worse than BFS (except for the case where an LRU-buffer is included), but it consumed less memory resources, since it needs linear space with respect to the height of the R*-trees. RBFS 310 was the worst alternative (although it uses recursion and it needs linear space) since it revisits internal nodes to follow a best-first order.

In [20], the performance of R*-trees and xBR-trees was compared for the most usual spatial queries, like 315 *Point Location, Window, Distance Range, K Nearest Neighbor* and *Constraint KNN* queries. The conclusions arising from this comparison showed that the two indexes were competitive. The xBR-tree is more compact and it is built faster than the R*-tree. The performance of the xBR-tree was higher for *PLQs, DRQs* and *WQs*, while the R*-tree was slightly better for *KNNQs* and needed less disk accesses for *CKNNQs*.

Finally, in [18] improvements of the xBR-tree (modified internal node structure and tree building process) were presented, leading to the xBR⁺-tree. An extensive performance studio (I/O efficiency and execution time) based on real and synthetic datasets was also presented, taking into account the tree building process and

the processing of single dataset queries, using the two Quadtrees-based structures. These results showed that the two trees are comparable regarding their building performance, however, the xBR⁺-tree was an overall winner regarding spatial query processing.

The main objective of this paper is to compare the xBR⁺-tree performance [18] (the best index structure of the *xBR-tree family*) against the performance of the most popular spatial access method of the *R-tree family*, the R*-tree and a non-overlapping member of this family, the R⁺-tree, considering the most representative spatial queries, where one or two indexes are involved and to highlight the performance winner, considering the characteristics of each query. Our contribution differs from [8] in the following aspects:

- We utilized a new dynamic, disk-resident, balanced Quadtree-based index structure (called xBR+-tree). In [8], a simple bucket Quadtree, a partially RAM-resident, unbalanced structure was utilized.
- The performance comparison is carried out for more spatial queries when one dataset is involved (PLQ, WQ, DRQ and CKNNQ) and when two datasets are involved (εDJQ), not only for the KNNQ and KCPQ (called K Distance Join Query in [8]).
- We have compared the xBR⁺-tree with the R⁺-tree also (an R-tree index based on disjoint decomposition of space), not only with the R^{*}-tree as in [8].
- We have used in our experiments two large *real* datasets from OpenStreetMap¹ with 5.8 and 11.5 million of 2d points, whereas in [8], the authors used *artificial* data from Palomar Observatory Sky Survey², choosing for their experiments just the first 2 millions of records from the original data (from around 90 millions) and for creating 2d points, the first two attributes of the 39 stored.

3. The R-tree Family

R-trees [27] are hierarchical, height balanced data structures, derived from B-trees [32] and designed to be used in secondary storage. R-trees are considered as excellent choices for indexing various kinds of spatial data (points, rectangles, line-segments, polygons, etc.) and

http://spatialhadoop.cs.umn.edu/datasets.html

²http://astronomy.mnstate.edu/cabanela/MAPS_Database/

have been adopted in known commercial systems (e.g. 375 Informix [33], Oracle Spatial [34, 35], MySQL [36], PostGIS [37, 38], etc.). They are used for the dynamic organization of a set of spatial objects represented by their Minimum Bounding Rectangles (MBRs). The MBR represents the smallest axes-aligned rectangle in which the spatial objects are contained. A 2d MBR is determined by two 2d points that belong to its faces, one that has the minimum and one that has the maximum coordinates (these are the endpoints of one of the diagonals of the MBR). Using the MBR instead of the exact geometrical representation of the object, its repre- 385 sentational complexity is reduced to two points where the most important features of the spatial object (position and extension) are maintained. Consequently, the MBR is an approximation widely employed, and the Rtrees belong to the category of data-driven access meth- 390 ods [1], since their structure adapts itself to the MBRs distribution in the space (the partitioning adapts to the object distribution in the embedding space).

The rules obeyed by the R-tree are as follows.

1. All leaves reside on the same level.

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- 2. Each leaf node contains entries, *E*, of the form (*MBR*, *Oid*), such that *MBR* is the minimum bounding rectangle that encloses the object determined by the identifier *Oid*.
- 3. Internal nodes contain entries, *E*, of the form (*MBR*, *Addr*), where *Addr* is the address of the child node and *MBR* is the minimum bounding rectangle that encloses MBRs of all entries in that child node (it is also called *directory MBR*).
- 4. Nodes (except possibly for the root) of an R-tree of class (m, M) contain between m and M entries, where $m \le \lceil M/2 \rceil$ (M and m are called maximum and minimum branching factor, or fan-out).
- 5. The root contains at least two entries, if it is not a leaf.

For more details about the R-tree structure, see [4].

Like other spatial tree-like index structures, an R-tree partitions the multidimensional space by grouping objects in a hierarchical manner. A subspace occupied by a tree node in an R-tree is always contained in the subspace of its parent node, i.e. the *MBR enclosure property*. According to this property, an MBR of an R-tree node (at any level, except at the leaf level) always encloses the MBRs of its descendant R-tree nodes. This property of spatial containment between MBRs stored in R-tree nodes is commonly used by spatial queries as the *WQ* and spatial join. Another important property of the R-trees that store spatial objects in a spatial database is the *MBR face property*. This property says

that every face of any MBR of an R-tree node (at any level) touches at least one point of some spatial object in the spatial database. Distance-based queries, like the KNNQ, DRQ, KCPQ and εDJQ , use this last property.

3.1. The R-tree*

Many variations of R-trees have appeared in the literature (exhaustive surveys can be found in [16, 4]). One of the most popular and efficient variations is the R*-tree [19]. The R*-tree is a variant of the R-tree that provides several improvements to the insertion algorithm. Essentially, these improvements aim at optimizing the following parameters: (1) node overlapping, (2) area covered by a node, and (3) perimeter of an MBR of internal node. The latter is representative of the shape of the rectangles because, given a fixed area, the shape that minimizes the rectangle perimeter is the square.

The R*-tree added two major enhancements to the Rtree, in case a node overflows. First, rather than just considering the area, the node-splitting algorithm in the R*-tree also minimized the perimeter and overlap enlargement of the MBRs. It tends to reduce the number of subtrees to follow for search operations. Second, the R*-tree introduced the notion of forced reinsertion to make the tree shape less dependent to the insertion order. When a node overflows, it is not split immediately, but a portion of entries of the node is reinserted from the tree root. The forced reinsertion provides two important improvements. First, it may reduce the number of splits and, second it is a dynamic technique for tree reorganization. With these two enhancements, the improved split algorithm and the reinsertion strategy, the R*-tree results in a much better organization with respect to the original R-tree.

It is worth remembering that the data structures for the R-tree and R*-tree are the same. Hence, the data retrieval operations defined for the R-tree remain valid for the R*-tree. Due to the better organization of the R*-tree, the performance of the spatial queries is likely to be significantly improved. For this reason, the R*-tree generally outperforms R-tree and it is commonly accepted that the R*-tree is one of the most efficient R-tree variants [1].

Figure 1 depicts a collection of points representing $16 \ capital \ cities$ and the corresponding R*-tree (assuming M=4 and m=2), where the tree nodes correspond to disk pages. Observe that the index structure, while keeping the tree balanced, adapts to the skewness of data distribution. Solid lines denote the MBRs of the subtrees that are rooted in inner nodes (dotted rectangles). In this figure, the leaves are represented by L_i ($1 \le i \le 6$), the MBRs enclosing points are denoted as

 I_i (1 $\leq i \leq$ 6) and R_i (1 $\leq i \leq$ 2) correspond to the MBRs enclosing I_i MBRs.

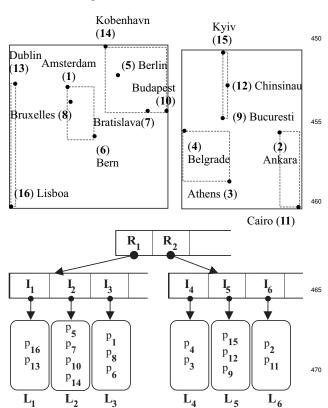


Figure 1: A collection of points representing 16 capital cities, the corresponding grouping to R*-tree nodes and the R*-tree structure.

3.2. The R^+ -tree

To overcome the problems associated with overlapping of regions in the R-trees, in [25] an access method called the R+-tree was introduced. The main motivation for the R⁺-tree is to avoid overlap among the MBRs. Unlike the R-tree, the R⁺-tree uses *clipping*; that is, there is no overlap between MBRs at the same tree level. MBRs that intersect more than one MBRs have to be stored on several different nodes. The result of this data structure is that there may be several paths, starting at the root to the same rectangle. As a result of this policy and taking into account its structure, the R+-tree will lead to an increase of the height of the tree. However, considering the retrieval time, point searches in R⁺-trees correspond to single-path tree traversals from the root to 490 one of the leaves (and therefore, it tends to be faster than the corresponding R-tree operation). On the other hand, range searches usually lead to the traversal of multiple paths in both index structures.

The R⁺-tree can be characterized as follows [1]:

- 1. The root has at least two entries, except when it is a leaf.
- The MBRs of two internal nodes at the same level cannot overlap.
- 3. If node *N* is not a leaf (internal node), its MBR contains all rectangles in the subtree rooted at *N*.
- 4. A rectangle of the collection to be indexed is assigned to all leaf nodes the MBRs of which it overlaps. A rectangle assigned to a leaf node *N* is either overlapping *N.MBR* or is fully contained in *N.MBR*. This duplication of objects into several neighbor leaves is similar to what we encountered earlier in other *space-driven structures* (they are based on partitioning the embedding space into rectangular cells, independently of the distribution of the spatial objects).

Figure 2 presents an R⁺-tree for the same collection of points. Note also that both at the leaf level and at internal levels, node MBRs are not overlapping (different organization of the nodes with respect to Figure 1). The notation of internal nodes and leaves are the same as in the R*-tree of Figure 1.

The structure of an R^+ -tree node is the same as that of the R-tree. However, because we cannot guarantee a minimal storage utilization m (as for the R-tree), and because rectangles are duplicated, an R^+ -tree can be significantly larger (in terms of height) than the R-tree built for the same dataset. The construction and maintenance of the R^+ -tree are rather more complex than with the other variants of the R-tree.

As examples of spatial query processing using R⁺-trees, the *point location query* performance benefits from the non-overlapping of nodes. As for *space-driven structures* [1], a single path down the tree is followed, and fewer nodes are visited than with the R-tree. The gain for *window query* is less obviously assessed. Object duplication not only increases the tree size, but potentially leads to expensive post-processing of the result (sorting for duplication removal).

4. The xBR⁺-tree

The xBR⁺-tree [18] (an extension of the xBR-tree [17, 20]) is a hierarchical, pointer-based, disk-resident index structure, built utilizing a regular decomposition of space (space-driven access method), suitable for indexing multidimensional points. For 2d the hierarchical decomposition of space in the xBR⁺-tree is that of Quadtrees (the space is recursively subdivided in 4

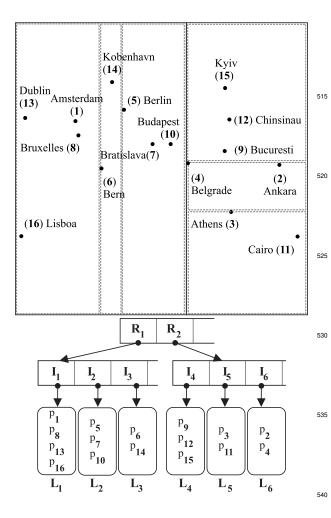


Figure 2: The same collection of points, the corresponding grouping to R^+ -tree nodes and the R^+ -tree structure.

equal subquadrants) and the space indexed is a *square*. The nodes of the tree are disk pages of two kinds: *leaves*, which store the actual multidimensional data themselves and *internal nodes*, which provide a multiway indexing mechanism.

4.1. Internal Nodes

Internal node entries in xBR⁺-trees contain entries of the form (Shape, qside, DBR, Pointer). Each entry corresponds to a child-node pointed by Pointer. The region of this child-node is related to a subquadrant of the original space. Shape is a flag that determines if the region of the child-node is a complete or non-complete square (the area remaining, after one or more splits; explained later in this subsection). This field is heavily used in queries. DBR (Data Bounding Rectangle) stores the coordinates of the rectangular subregion of the child-node

region that contains point data (at least two points must reside on the sides of the *DBR*), while *qside* (not stored in xBR-tree internal node entries) is the side length of the subquadrant of the original space that corresponds to the child-node.

The subquadrant of the original space related to the child-node is expressed by an Address. This Address (which has a variable size) is not explicitly stored in the xBR⁺-tree (unike the xBR-tree), although it is uniquely determined and can be easily calculated using *qside* and DBR (in fact, the coordinates of the subquadrant expressed by Address are calculated by query processing algorithms using *qside* and *DBR*). Each *Address* represents a subquadrant which has been produced by Quadtree-like hierarchical subdivision of the current space (of the subquadrant of the original space related to the current node). It consists of a number of directional digits that make up this subdivision. The NW, NE, SW and SE subquadrants of a quadrant are distinguished by the directional digits 0, 1, 2 and 3, respectively. For 2d space, we use two directional bits, one for each dimension. The lower bit represents the subdivision on the horizontal (X-axis) dimension, while the higher bit represents the subdivision on the vertical (Y-axis) dimension [17, 20]. It is easy to extend this representation to three or more dimensions by using a number of directional bits equal to the number of dimensions. For example, the Address 1 represents the NE quadrant of the current space, while the Address 10 the NW subquadrant of the NE quadrant of the current space. The address of the left child is * (has zero digits), since the region of the left child is the whole space minus the region of the right child.

However, the actual region of the child-node is, in general, the subquadrant of its Address minus a number of smaller subquadrants, the subquadrants corresponding to the next entries of the internal node (the entries in an internal node are saved sequentially, in preorder traversal of the Quadtree that corresponds to the internal node). For example, in Figure 3 an internal node (a root) that points to 2 internal nodes that point to 7 leaves is depicted. The region of the root is the original space, which is assumed to have a quadrangular shape. The region of the right child is the NW quadrant of the original space. The region of the left child is the whole space minus the region of the NW quadrant, a non-complete square. The * symbol is used to denote the end of a variable size address. The Address of the right child is 0*, since the region of this child is the NW quadrant of the original space. The Address of the left child is * (has zero directional digits), since the region of this child refers to the remaining space. Each of these Addresses is expressed relatively to the minimal quadrant that covers the internal node (each Address determines a subquadrant of this minimal quadrant). For example, in Figure 3, the Address 3* is the SE subquadrant of the NW subquadrant of whole space (absolute Address 03*). During a search, or an insertion of a data element with specified coordinates, the appropriate leaf and its region is determined by descending the tree from the root

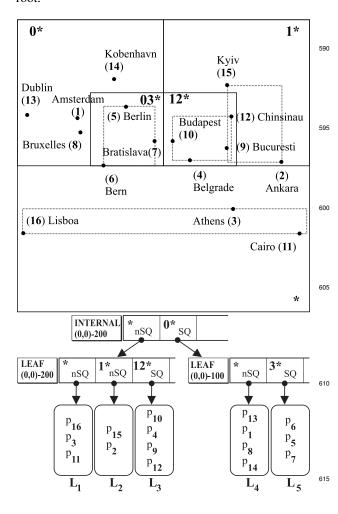


Figure 3: The same collection of points, the corresponding grouping to xBR+-tree nodes and the xBR+-tree structure.

Note that all the fields of an xBR⁺-tree internal node entry have a fixed size. By avoiding storing the variable-sized field *Address* (unlike the xBR-tree), processing of internal nodes is simplified, since their capacity is fixed. Moreover, the use of the *DBR* field (not stored in xBR-tree internal node entries) makes processing of spatial queries more efficient, since it signifies the subregion of the child-node that actually contains data, which is (in

general) different to and smaller than the region of this child-node, leading to higher selectivity of the paths that have to be followed downwards when descending the tree and deciding the parts of the tree that may contain (part of) the query answer.

4.2. Leaf Nodes

External nodes (leaves) of the xBR⁺-tree simply contain the data elements and have a predetermined capacity C. When C is exceeded, due to an insertion in a leaf, the region of this leaf is partitioned in two subregions. The one (new) of these subregions is a subquadrant of the region of the leaf which is created by partitioning the region of the leaf according to hierarchical (Quadtree like) decomposition, as many times as needed so that the most populated subquadrant (that corresponds to this new subregion) has a cardinality that is smaller than or equal to C. The other one (old) of these subregions is the region of the leaf minus the new subregion. In [18], the criterion of choosing the new subregion was the cardinality of this subregion to be smaller or equal to xC, where 0.5 < x < 1, however the criterion we use in this paper was more effective and simple. Note also that in the xBR⁺-tree, data elements are stored in leaves in X-order (the elements are sorted in ascending order of their X-axis coordinate). This order permits us to use the *plane sweep* technique (when appropriate) during processing of the data elements of a leaf, in the process of answering certain query types.

4.3. Splitting Process of Nodes

When an internal node of the xBR⁺-tree overflows, it is split in two. The goal of this split is to achieve the best possible balance between the space use in the two nodes.

4.3.1. Splitting of internal nodes

The split in the xBR⁺-tree is either based on existing quadrants or in ancestors of existing quadrants. First, a Quadtree is built that has as nodes the quadrants specified in the internal node [17]. This tree is used for determining the best possible split of the internal node in two nodes that have almost equal number of bits, as proposed in [17], or entries (a simpler and equally effective criterion, according to experimentation).

4.3.2. Splitting of leaves

Splitting of a leaf creates a new entry that must be hosted by an internal node of the parent level. This can cause backtracking to the upper levels of the tree and may even cause an increase of its height. More details appear in [17].

5. Spatial Ouery Processing

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In this section, we outline algorithms for processing 675 *PLQs*, *WQs*, *DRQs*, *KNNQs*, *CKNNQs*, *KCPQs* and *&DJQs* on the R-tree family (query processing in R*-trees, R*-trees and R-trees, in general, is similar) and xBR*-trees. In general terms, the definitions of these spatial queries are as follows:

- Given an index I_P and a query point q, the **PLQ** 680 returns true if q belongs to I_P , false otherwise.
- Given an index I_P and a query rectangle r, the result of the WQ is the set of all points in I_P that are completely inside r.
- Given an index I_P , a query point q and a distance threshold $\varepsilon \geq 0$, the **DRQ** returns all points of I_P , that are within the specified distance ε from q (according to a distance function).
- Given an index I_P, a query point q, and a value K > 0, the KNNQ returns K points of I_P which are closest to q based on a distance function.
 - Given an index I_P , a query point q, a value K > 0 695 and a distance threshold $\varepsilon \ge 0$, the CKNNQ returns K closest points of I_P which are within the distance ε from q.
 - Given two indexes I_P and I_Q , and an integer value K > 0, the K**CPQ** [39, 40] returns a set of K different pairs of points $(p_i, p_j) \in I_P \times I_Q$, such that $p_i \in I_P$, $p_i \in I_Q$, with the K smallest distances between all possible pairs of points that can be formed by choosing one point of I_P and one point of I_Q , based on a distance function.
- Given two indexes I_P and I_Q , and a real value $\varepsilon \ge 0$, $\varepsilon \mathbf{DJQ}$ [31] returns all the possible different pairs of points $(p_i, p_j) \in I_P \times I_Q$ that can be formed by choosing one point $p_i \in I_P$ and one point $p_j \in I_P$, 710 having a distance smaller than or equal to ε of each other, based on a distance function.

To answer the aforementioned spatial queries using members of the R-tree family, or xBR⁺-trees a two-step procedure is followed [41]. *Filter step*: the collection of all spatial objects whose MBRs/DBRs satisfy the given spatial query is found. These spatial objects constitute the candidate set. *Refinement step*: the actual exact geometry of each member of the candidate set is examined to eliminate false hits and find the final answer to the spatial query. In the following, we will describe in more

detail the query processing techniques that have developed for each spatial query type. Since the *Refinement step* is orthogonal to the *Filtering step*, the developed techniques have mainly focused on the latter.

5.1. Algorithmic techniques used

All the single dataset queries above can be processed in a top-down manner beginning from the root of the tree. There are two, well known, basic techniques that can be applied.

The first one is processing the nodes of the tree in Depth-First (DF) mode: By examining the relation of an entry of the current internal node to the query object, point or area, we decide on recursively applying the same procedure on the child node pointed by this entry. When this recursive call returns, another entry of this internal node may be examined, depending on the query being processed and the result calculated so far. When a recursive call reaches a leaf node, the *Refinement step* is applied.

The second one is processing the nodes of the tree in Best-First (BF) mode: By examining the relation of each entry of the current internal node to the query object, point or area, we decide about inserting this entry in a global priority queue, where there may already exist entries inserted during earlier stages of the algorithm. After all entries of the current node have been examined, the entry with top priority is extracted from the queue and processing continues with the node pointed by this entry.

We applied four versions of DF algorithms.

- The first one, named Normal Depth First (N-DF) algorithm, is the simplest of all. The query object is tested first against each entry of the current node, in the order that the entries are stored. The criterion for such a test depends on the query being processed and the result calculated so far and its result is boolean (true / false). If the result for the entry tested is true, then the algorithm is applied recursively on the child node pointed by this entry.
- The second one is named Depth First (DF) algorithm. For each entry of the current node (in the order that the entries are stored), the minimum distance, *mindist*, between the query object and the region of the entry is calculated. If the (non-boolean) value of this metric for the entry examined satisfies the criterion corresponding to the query being processed and the result calculated so far, then the algorithm is applied recursively on the node pointed by this entry.

• The third one, named Sorted Depth First (S-DF) algorithm, is a fairly used and efficient DF technique. There is an initial step that must be implemented when an internal node is visited, so as to select the entry of this node that best satisfies the criterion corresponding to the query being processed and the result calculated so far. In this step, for all entries of the current node, *mindist(q, M)* values are calculated, inserted in an array and sorted. Then the algorithm is applied recursively on the node pointed by the entry corresponding to the lowest *mindist* value. When this recursive call returns, recursion is possibly (depending on the query being processed and the result calculated so far) applied on the entry with the next *mindist* value.

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• The fourth one, named Heap Depth First (H-DF) algorithm, is a new technique that utilizes one local (to the current node) minimum Heap (*minHeap*) prioritized by the *mindist* metric. The *minHeap* replaces the sorted array of S-DF and this is expected to speed up the selection process of the next best entry for applying recursion. In fact, the fewer the entries of the current node that will be eventually used for recursive calls, the more the algorithm will accelerate (since extracting from *minHeap* part and not all of its entries corresponds to a partial application of HeapSort, in contrast to always completely sorting the respective array of S-DF).

We also applied one BF algorithm.

- In the following, this is called BF algorithm and it is iterative. It keeps a global (to the whole tree) minimum binary heap, minHeap, holding (part of) the entries of the nodes visited so far, priori-805 tized by their mindist to the query object. Initially, minHeap contains the tree root. Iteratively, the entry at the root of minHeap is removed from the heap and the node pointed by this entry is visited; its entries are potentially added to the heap, according to the relation of mindist of each entry to the 810 criterion of the query being processed and the result calculated so far. The algorithm continues by visiting the node pointed by the entry with the minimum mindist in minHeap until the heap becomes empty or the mindist value of the entry located in the root of the heap does not satisfy the criterion corresponding to the query being processed and the result calculated so far. When the algorithm reaches a leaf node, the *Refinement step* is applied.
- All the dual dataset queries above can be processed in 820 a top-down manner by synchronous tree traversals, be-

ginning from the roots of the two trees. Again, the basic ideas of processing the nodes of the trees in DF and BF mode are utilized.

We applied three versions of DF algorithms for dual dataset queries. N-DF cannot be applied, due to its boolean criterion. We did not apply a version analogous to DF, since, when the entries of two nodes (one from each tree representing a different dataset) are combined, the number of combinations that should be examined is large, unless a technique that reduces the number these combinations is applied. Thus, we applied versions analogous to S-DF and H-DF, only.

- The first one, is named Sorted Depth First for 2 datasets (S-DF-2) algorithm. We start at the roots of the two trees (current pair of nodes). For each pair of entries formed by combining the entries of the current pair of nodes, the minimum distances, mindist values, between the regions of the elements of the pair are calculated (these are distances between rectangular regions), inserted in an array and sorted. Then the order of this array is used for recursive application of the algorithm. If mindist of the next array entry (a pair of nodes) satisfies the criterion corresponding to the query being processed and the result calculated so far, then the algorithm is applied recursively on the nodes pointed by the elements of this pair. In case a recursive call reaches a pair of nodes where one of its elements is a leaf, then the pairs of entries are formed by the region of this leaf and the entries of the node pointed by the other element of the pair (which is an internal node). In case a recursive call reaches a pair of nodes where both of its elements are leafs, the Refinement step is applied.
- The second one, named Heap Depth First for 2 datasets (H-DF-2) algorithm, is a new technique that utilizes one local (to the current pair of nodes) minimum Heap (minHeap) prioritized by the mindist metric that replaces the sorted array of S-DF-2. For the reasons described above, this algorithm is expected to speed up the selection process of the next best entry for applying recursion.
- The third one, is named Classic Plane Sweep Depth First for 2 datasets (C-DF-2) algorithm. In this algorithm, when a pair of nodes is visited, for each node of this pair, the starting coordinate of one of the axes, w.l.o.g. let's assume this is *x*-axis, of the rectangular regions of this node entries are sorted and Classic Place Sweep [42] is applied between the two sorted coordinate sequences. If *x*-

distance of the pair of entries under examination is smaller than the current threshold corresponding to the query being processed and the result calculated so far, then the actual mindist is calculated for 875 this pair of entries and, if the calculated value satisfies the criterion corresponding to the query being processed and the result calculated so far, the algorithm is applied recursively on the nodes pointed by the elements of this pair. Unlike S-DF-2 and H-DF-2, this algorithm avoids unnecessary calculations of mindist values. Note that in C-DF-2, when a recursive call reaches a pair of nodes where one of its elements is a leaf, plane sweep is not applied (plane sweep makes sense when two sets of rectangular regions are combined), but the region of this leaf is combined with all the entries of the other node.

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We also applied one BF algorithm for dual dataset 890 queries.

• This is called Classic Plane Sweep Best First for 2 datasets (C-BF-2) algorithm and also utilizes Classic Place Sweep [42]. This algorithm is iterative. It 895 keeps a global (to the whole pair of trees) minimum binary heap, minHeap, holding (part of) the pairs of entries of the pairs of nodes visited so far, prioritized by their mindist. Initially, minHeap contains the two tree roots. Iteratively, the entry at 900 the root of minHeap is removed from the heap and the pair of nodes pointed by this entry is visited. For the pairs of entries formed from this pair of nodes plane sweep is applied, like in C-DF-2 and, each pair of entries that satisfies the criterion corresponding to the query being processed and the result calculated so far is inserted in minHeap. The algorithm continues by visiting the pair of nodes pointed by the pair of entries with the minimum mindist in minHeap until the heap becomes empty or the mindist value of the pair of entries located 910 in the root of the heap does not satisfy the criterion corresponding to the query being processed and the result calculated so far. In case the algorithm visits a pair of nodes where one of its elements is a leaf, then the pairs of entries are formed by the re- 915 gion of leaf and the entries of the node pointed by the other element of the pair (which is an internal node) and plane sweep is not applied, but the region of this leaf is combined with all the entries of the other node. In case the algorithm visits a pair 920 of nodes where both of its elements are leafs, the Refinement step is applied.

5.2. Point Location and Window Queries

PLQs and WQs can be processed using N-DF algorithm on both the R-tree and xBR+-tree families. The query object in the case of *PLQs* is the query point and the testing criterion is whether there is overlapping between the query point and the the MBR/DBR of the current entry of the R-tree/xBR+-tree. The query object in the case of WQs is the query window (rectangle) and the testing criterion is whether there is intersection between the query window and the the MBR/DBR of the current entry. Since the criterion can only get one of two possible values TRUE/FALSE, there is no way or reason the values of the criterion to be compared between entries. When the node pointed by the Addr is a leaf then Refinement step is applied. For PLQs, the query point is searched between the points of the leaf and if it is found the result is returned in the calling procedure in order the searching process to be terminated. For WQs, the set of points of the current leaf within the query window are found and this set of points is returned. The searching process will be terminated when all entries of the root node have been tested.

Especially for the xBR⁺-tree, as noted in Subsection 4.1, the entries in an internal node are saved in preorder traversal of the Quadtree that corresponds to the internal node and are examined in reverse sequential order (this means that first a subregion is examined before any enclosing region of this subregion, and in this way, multiple examinations of overlapping regions are avoided). So the last entry of the current internal node is examined first. Moreover, for the xBR⁺-tree, in *WQs* a termination condition can be applied and the searching process can be terminated before all entries of the current node have been tested: whenever the query window is contained within the *REG* of the current entry of the node processing stops. This is due to no overlapping between regions of the nodes.

5.3. Distance Range Queries

DRQs can be performed with all variants of DF and BF algorithms that were described above in Subsection 5.1 on both the R-tree and xBR⁺-tree families. The query object is a circle centered on the query point with radius a given value ε . Since in N-DF algorithm the testing criterion is whether there is intersection between the query circle and the MBR/DBR of the current entry, in order to simplify processing, the query circle is replaced by its MBR in the *Filter step*, while in the *Refinement step* the points inside the actual query circle are selected. Especially for the xBR⁺-tree, the same termination condition noted in Subsection 5.2 can be applied in the N-DF algorithm.

For the other four algorithms (DF, H-DF, S-DF and BF) the query object is the circle described above and *mindist* is the distance between the center of the query circle and the MBR/DBR of the current entry. The testing criterion is whether this *mindist* value is smaller than or equal to ε . The special termination condition of the xBR⁺-tree for the DF algorithm can be applied just like the N-DF one, while for the other three algorithms (S-DF, H-DF and BF) it must be partially changed, since the examination of the entries is not in the reverse order in which they are saved in the node. Thus, if the query circle is contained in the *REG* and the region of the entry is a complete square then the termination condition sets applied.

5.4. Nearest Neighbor Queries

Based on the branch-and-bound paradigm, the *K* Nearest Neighbor Query algorithms use several metrics to prune the search space [43]. The most important metric is *mindist*, the minimum distance between the query object and the region of the entry under examination. Another metric, *minmaxdist*, refers to the minimum distance from the query object within which a point in the region of the entry under examination is guaranteed to be found. Finally, *maxdist* is the maximum distance between the query object and any point in the region of the entry under examination.

The first Nearest Neighbor Query (NNQ) algorithm for R-trees, proposed in [43], traverses the tree recursively in a DF manner. Starting from the root, all entries are sorted according to their mindist from the query object, and the entry with the smallest mindist is visited first. The process is repeated recursively until the leaf level is reached, where a potential NN is found. During backtracking to the upper levels, the algorithm only visits entries whose mindist is smaller than or equal to the distance of the NN found so far. This algorithm was enhanced in [44], proving that any node can be pruned by using minmaxdist [43] distance function. A BF al- 1010 gorithm for NNQ was proposed in [45] for Quadtrees and in [46] for R-trees. BF keeps a minimum binary heap, minHeap, with the entries of the nodes visited so far, prioritized according to their mindist. Initially, minHeap contains the entries of the tree root. When the root of minHeap is chosen for processing, it is re- 1015 moved from the heap and the entries of its tree node are added to the heap. The algorithm continues visiting the entry with the minimum mindist in minHeap, until the heap becomes empty or the mindist value of the node entry located in the root of heap is larger than 1020 the distance value of the nearest neighbor that has been

found so far (i.e. the pruning distance). BF is I/O optimal because it only visits the nodes necessary for obtaining the NN. The generalization to find the *K* Nearest Neighbor (*K*NN) is straightforward. An additional data structure is just needed, a maximum binary heap, maxKHeap (prioritized by the distance from the query point), holding the *K* nearest points encountered so far.

It is obvious that the four algorithms (DF, S-DF, H-DF and BF) described in Subsection 5.1 can be adapted to *KNNQs* on both the R-tree and xBR⁺-tree families. The query object is the circle centered at the query point and having radius equal to the key of the root of the full *maxKHeap*; otherwise (not full *maxKHeap*) this circle covers the whole space. The testing criterion (*Filter step*) is whether there is an intersection between the query circle and the *MBR/DBR* of the current entry; in the *Refinement step* the points inside the actual query circle are selected.

Especially for the xBR⁺-tree, the same termination condition noted in Subsection 5.3 can be applied in the algorithms for *KNNQs*; when the region of the current entry is square and contains the query circle then the process is terminated. More details about this algorithm appear in [20, 47].

The CKNNQ is a combination of the KNNQ and DRQ; for this uery, we can adapt the DF, S-DF, H-DF or BF algorithms for NNQ on both the R-tree and xBR^+ -tree families. The query object is the circle with center the query point and radius the given maximum ε value for the case of not full maxKHeap, otherwise the radius is the key of the root of the full maxKHeap. The testing criterion ($Filter\ step$) is whether there is intersection between the query circle and the MBR/DBR of the current entry in the $Filter\ step$; in the $Refinement\ step$ the points inside the actual query circle are selected. Especially for the xBR^+ -tree, the same termination condition can be applied as in the the NNQ algorithms.

5.5. Distance Join Queries

Be reminded that the *KCPQ* asks for the *K* closest pairs of spatial objects in the Cartesian Product of two datasets. If both datasets are indexed by R-trees, the concept of synchronous tree traversal and DF or BF traversal order can be combined for query processing [29, 39, 48, 40]. Details on such DF and BF algorithms on two R*-trees, from the non-incremental point of view, using several optimization techniques (i.e. planesweep, distance functions like *minmaxdist* and *maxdist*) appear in [40]. In the following, we outline the distance join algorithms we applied on all the three trees.

- For *KCPQs*, we applied all the four algorithms S-DF-2, H-DF-2, C-DF-2 and C-BF-2 described 1070 in Subsection 5.1. The testing criterion is based on the distance threshold which is, either equal to the key of the root of the *maxKHeap*, in case of a full *maxKHeap*, or to an infinite length, in case of a non-full *maxKHeap*. The testing criterion is whether the distance of the pair objects (*MB R/DBR*) under examination is smaller than the distance threshold. In the *Refinement step* (when the algorithm visits a pair of leaves), Classic Plane Sweep is applied between the points of the two 1080 leaves. If a pair of points consists of points with a distance smaller than the distance threshold, this pair is inserted in *maxKHeap*.
- For the εDJQ ($\varepsilon \ge 0$), the above DF or BF algorithms for KCPQ (for all trees) are adapted in a straightforward way. There is no maxKHeap, or limit on the cardinality of the result and the distance threshold always equals ε . Starting from the root nodes, tree nodes are traversed down to the leaves, depending on the result of whether mindist of the pair of entries under examination is less than or equal to ε . When the algorithm reaches a pair of leaves, Classic Plane Sweep is applied between the points of the two leaves. All the pairs of points with a distance smaller than or equal to ε are added to the answer set.

These algorithms (except for H-DF-2, which is new) have been proposed in the past for the R-tree family. However, algorithms for the KCPQ and the εDJQ have 1100 not been presented for the xBR⁺-tree before. In this work, we adapted the existing R-tree algorithms and applied the H-DF-2 technique on the specific structure of xBR⁺-tree.

6. Experimentation

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We designed and run a large set of experiments to compare xBR⁺-trees with respect to R-tree variants (R*-tree and R⁺-tree).

6.1. Experimental Settings

We used 6 real spatial datasets of North America, representing cultural landmarks (NAclN with 9203 points) and populated places (NAppN with 24491 points), roads (NArdN with 569082 line-segments) and rail-roads (NArrN with 191558 line-segments). To create sets of 2d points, we have transformed the MBRs of line-segments from NArdN and NArrN into points by taking

the center of each MBR (i.e. |NArdN| = 569082 points, |NArrN| = 191558 points). Moreover, in order to get the double amount of points from NArrN and NArdN, we chose the two points with min and max coordinates of the MBR of each line-segment (i.e. |NArdND| = 1138164 points, |NArrND| = 383116 points). The data of these 6 files were normalized in the range $[0, 1]^2$. We have also created synthetic clustered datasets of 125000, 250000, 500000 and 1000000 points, with 125 clusters in each dataset (uniformly distributed in the range $[0,1]^2$), where for a set having N points, N/125 points were gathered around the center of each cluster, according to Gaussian distribution. We have also used two large real spatial datasets (retrieved from http://spatialhadoop.cs.umn.edu/datasets.html [49]) to justify the use of spatial query algorithms on diskresident data instead of using them in-memory. They represent water resources of North America (Water) consisting of 5836360 line-segments and parks or green areas of all world (Park) consisting of 11504035 polygons. To create sets of points, we have transformed the MBRs of line-segments from Water into points by taking the center of each MBR and we have considered the centroid of polygons from Park.

The experiments were run on a Ubuntu Linux v. 14.04 machine with Intel core duo 2x2.8 GHz processor, 4 GB of RAM and a Seagate Barracuda 3TB SATA 3 hard disk, using the GNU C/C++ compiler (gcc).

For page (node) sizes of 1KB, 2KB, 4KB, 8KB and 16KB we run experiments for tree building, counting tree characteristics and creation time and experiments for all spatial queries studied here (*PLQ*, *WQ*, *DRQ*, *KNNQ*, *CKNNQ*, *KCPQ* and *&DJQ*), counting disk read accesses (I/O) and total execution time (I/O and CPU).

6.2. Experiments for comparing index structures

In these experiments, we built the xBR⁺-tree, the R*-tree and the R⁺-tree. We constructed each tree, using LRU-buffer¹ of 1024 pages. For each dataset, the insertion order of the data was the same for all trees. In Table 1, construction characteristics of the three trees, for a representative set of dataset and node size combinations (for the sake of presentation length), are depicted.

Regarding tree heights, studying the complete set of construction characteristics of the three trees (for all dataset and node size combinations), we conclude that:

• The xBR⁺-tree and R*-tree have similar tree heights.

¹The improvement of the creation times of the xBR⁺-tree in relation to the respective creation times in [18] is due to the use of the LRU-buffer.

	Num	Node	Tree	heig	ht	Tree	size (ME	Bytes)	Crea	tion time	(secs)
Dataset	Elem (×10 ³)	size (KB)	xBR ⁺	R*	R ⁺	xBR ⁺	R*	R ⁺	xBR ⁺	R*	R ⁺
NAclN	9.203	1	4	4	4	0.615	0.669	0.652	0.0511	0.3119	0.1252
NAppN	24.491	1	4	4	4	1.600	0.820	1.718	0.2286	1.0239	0.2663
NArrN	191.558	2	4	4	4	11.61	13.47	12.39	2.5324	15.385	2.8480
NArrND	383.180	4	4	3	4	22.78	26.82	24.03	6.5064	86.771	8.0914
NArdN	569.082	8	3	3	3	34.73	40.67	34.97	12.112	461.78	19.558
NArdND	1138.19	16	3	3	3	69.31	82.10	67.95	39.606	3450.7	66.697
125KCN	125.000	2	4	4	4	7.578	7.984	7.242	1.0643	8.6246	1.5947
250KCN	250.000	4	3	3	3	15.09	15.90	14.23	2.9603	46.682	4.5291
500KCN	500.000	8	3	3	3	30.02	31.83	28.06	8.5643	339.39	15.969
1000KCN	1,000.00	16	3	3	3	59.33	63.49	56.19	28.882	2360.6	60.635
Water	5,836.36	2	5	5	11	359.2	438.1	395.4	114.97	584.23	286.98
Water	5,836.36	4	4	4	5	352.9	443.6	382.3	139.92	1638.6	262.23
Park	11,504.0	8	4	4	4	684.0	839.7	731.6	402.91	9460.3	947.12
Park	11,504.0	16	3	3	3	682.7	855.5	719.0	565.42	37174	1240

Table 1: Tree construction characteristics.

• The R⁺-tree for the large real spatial datasets and the smaller node sizes (1KB and 2KB) is signifi- 1145 cantly higher.

This is due to the fact that the R⁺-tree, to avoid overlapping, in many cases, splits internal nodes and several of their descends at subsequent levels, creating nodes with limited occupancy. For a smaller node size, an internal node is more likely to be split unevenly and the 1150 new node with the smaller occupancy may not increase significantly its occupancy in the future, if there are not enough new data within its region. This shows the sensitivity of the R⁺-tree to the order of insertion of the data.

Regarding tree sizes, the three trees have similar $_{1155}$ sizes, since the largest part of each tree consists of leaves and the leaves exhibit similar occupancy in all trees (average leaf occupancy of the xBR⁺-tree, the R^{*}-tree and the R⁺-tree is 65.14%, 68.24% and 65.14%, respectively). In conclusion:

- For real datasets the xBR⁺-tree needs less space in disk (i.e. it is more compact).
- For synthetic datasets the R⁺-tree has the smallest disk size.

Regarding creation times:

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• The xBR⁺-tree is always the fastest.

This is due to the regular way that the xBR⁺-tree divides the space. Moreover, node splitting follows a single path, starting from the leaf level and ending, on the

worst case, at the root level. On the contrary, in the R⁺-tree splits may be propagated to parent, as well as, to children nodes [25].

• The R*-tree is always the slowest.

This is due to forced reinsertion and the multiple paths while searching for the appropriate leaf that will host the new point [19].

6.3. Creation of input for queries on single datasets

We split the whole space into 2^4 , 2^6 , ..., 2^{16} equal rectagular windows, in a row-order mapping manner. These windows were used as query windows for WQs. The centroids of these windows were used as query points PLQs, K-NNQs and CK-NNQs. The incircles of these windows were used as query ranges for DRQs (the centroid of each of these windows was used as the center of a query range and the extend of this range, ε , was equal to the half of the side length of this window). For K-NNQs and CK-NNQs, we used the set of K values $\{1, 10, 100, 1000\}$.

6.4. Experiments for non distance-based queries on single datasets (PLQs and WQs)

As the number of experiments performed was huge, we show only representative results, since they were analogous for each query category. For *PLQs* we executed two sets of experiments using the N-DF algorithm. In the first set we used as query points the original datasets and in the second one we used as query

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points the centroids of the query windows. Indicative results for the *Water* dataset are shown in Figures 4.a (I/O) and 4.b (execution time) and for the $1000KCN_{1220}$ dataset are shown in Figures 4.c (I/O) and 4.d (execution time).

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These figures show that the results are different for the two cases of experiments. For the case of the query shown in Figures 4.a and 4.b (Water), when searching 1225 for an existing point into the spatial dataset, the number of disk read accesses needed by the R^+ -tree and the xBR $^+$ -tree is equal to the tree height. On the other hand, the number of disk read accesses for the R^* -tree is a little larger than the height of the tree. The execution time 1230 of R^* -tree is smaller than the one of the R^+ -tree and a little larger than the one of the xBR $^+$ -tree.

Studying the complete set of results of PLQs using as query points the original datasets, we find out that the same situation appears. Regarding I/O, we conclude 1235 that:

- For both the xBR⁺-tree and the R⁺-tree, the number of disk read accesses is equal to the height of the tree for every query point, if this point exists in the dataset, because of the single path that has to be followed until this point is found.
- For the R*-tree, the number of disk read accesses is a little larger than the height of the tree because of the multiple paths that are possibly needed to be 1245 followed until the point is found.

Summarizing the results for the execution time:

- The xBR⁺-tree was faster than the R⁺-tree in all cases (60/60) and faster than the R^{*}-tree in most cases (56/60).
- The R*-tree was faster than the R*-tree in all cases, for all datasets and node sizes.
- Especially, for the node size of 16KB, the xBR⁺-tree needed fewer disk read accesses for all datasets, with an average relative difference of 5.75% to the R*-tree.
- Moreover, it was faster for all datasets (12/12) with ¹²⁵⁵ an average relative difference of 70.9% to the R*tree.

For the case of the experiment shown in Figures 4.c and 4.d (1000KCN dataset), the number of disk read ac- 1260 cesses needed by the R⁺-tree when searching for a point non-existing in the spatial dataset is equal to the tree height. Note that for this dataset, the tree height of the R⁺-tree, the R^{*}-tree and the xBR⁺-tree equals 6, 5, 6 for

1KB nodes, 4, 4, 5 for 2KB nodes, 4, 4, 4 for 4KB nodes and 3, 3, 3 for 8KB and 16KB nodes, respectively. In the case of the xBR+-tree, the number of disk read accesses needed is less than the tree height for most query points. In the case of R*-tree, the number of disk read accesses depends on the size of the empty space in relation to the occupied space (inside MBRs) and is larger than the tree height for all node sizes. Studying the results for the execution time, we note that there is a fairly constant difference in favor of the xBR+-tree against the other two trees. This query (PLQ) is related to the tree height and the size of MBRs that enclose the data points. So it seems easier for the R*-tree to decide that the query point does not exist in the dataset, than for the xBR+tree. But this fact is not enough to make the R*-tree faster than the xBR⁺-tree, since CPU processing of the tree structure is lighter for the xBR⁺-tree.

Studying the complete set of results of *PLQs* using as query points the centroids of the query windows, we find out that for R*-trees, the number of disk read accesses is smaller than the height of the tree for all real datasets, while for synthetic datasets this number is larger than the height of the tree. For R⁺-trees, the number of disk read accesses is always equal to the height of the tree because there is no overlapping between its leafs. For xBR⁺-trees, the number of disk read accesses is always smaller than the tree height. Summarizing I/O results, we find out that:

- The R*-tree needed the smallest number of disk read accesses in most cases (41/60).
- The xBR⁺-tree needed the smallest number of disk read accesses in 18/60 cases.
- Only in one case the R⁺-tree needed the smallest number of disk read accesses.

The results for the execution time showed that:

 The xBR⁺-tree is faster for all datasets and node sizes (60/60).

The WQ was executed using the N-DF algorithm, for all datasets (12) and all node sizes (5), searching for the points residing inside the query windows of various sizes (6). The results of the WQ for the NArdND dataset, using 2^{12} windows that cover the whole data space, regarding the number of disk read accesses per query (Table 2) and the execution time vs. the node size (Table 2 and Figure 5.a) are shown as a representative case. The use of the table is preferred due to the large difference of values between R^+ -tree and the other two

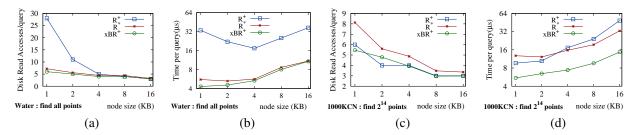


Figure 4: *PLQ*: disk read accesses (a) and exec. time (b) vs. node size (*Water*) with query points all dataset points and disk read accesses (c) and exec. time (d) vs. node size (1000*KCN*) with query points the centroids of the query windows.

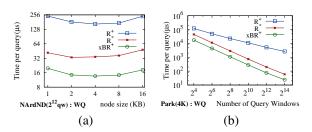


Figure 5: WQ: exec. time vs. (a) node size (NArdND, 2^{12} , query windows) and (b) number of query windows (Park with node size=4K).

Node	Disk Read Accesses			Exec	Execution Time (µs)		
Size	R^+	R*	xBR^+	R^+	R*	xBR ⁺	
1	144.4	24.60	21.81	241.6	41.62	19.72	
2	69.05	13.82	11.71	182.7	33.40	14.39	
4	36.33	9.049	7.039	165.0	34.19	13.62	
8	20.75	5.714	4.113	173.0	36.38	14.30	
16	14.71	4.267	3.139	239.5	47.98	18.31	

Table 2: WQ: disk read accesses and exec. time per query on NArdND (2^{12} query windows) vs. node size.

trees, especially for the cases of small node sizes (1KB, $_{1295}$ 2KB).

1265

In Table 2, it is shown that the xBR⁺-tree needed fewer disk read accesses (Acc) than the other two trees. As the node size increases, the absolute I/O difference between the trees becomes smaller, but the relative difference $(Acc_{R^+} - Acc_{R^*})/Acc_{R^+}$ has values (0.83, 0.80, 0.75, 0.72, 0.71) that are all in favor of R*-tree, while the relative difference $(Acc_{R^*} - Acc_{xBR^+})/Acc_{R^*}$ has values (0.11, 0.15, 0.22, 0.28, 0.26) that are all in favor of xBR+-tree. Note the reduction of the difference from the smallest node size (1KB) to the largest size (16KB). This is due to the reduction of tree height, as the node size increases. In Table 2 and in Figure 5.a, it is shown that the xBR+-tree is the fastest and the R*-tree is faster than the R⁺-tree, for all node sizes. All three trees needed less total execution time (I/O and CPU) for the node size equal to 4KB, even though larger node sizes needed fewer disk read accesses.

The results of the WQ on the large dataset Park in- 1310

Number	Disk	Disk Read Accesses			Execution Time		
Query	R ⁺	R*	xBR ⁺	R ⁺	R*	xBR^+	
Wins	$\times 10^3$	$\times 10^3$	$\times 10^{3}$	μ s	μ s	μ s	
24	26.18	11.38	11.085	120,510	44,651	17,375	
2^{6}	10.71	2.865	2.773	49,653	11,272	4,338	
2^{8}	4.869	0.726	0.695	22,350	2,861	1,088	
2^{10}	2.312	0.188	0.175	10,997	739.0	280.6	
2^{12}	1.122	0.051	0.045	5,170	198.4	75.09	
2^{14}	0.555	0.015	0.013	2,638	59.18	24.91	

Table 3: WQ: disk read accesses and exec. time per query on Park (node size=4KB) vs. number of Query Windows.

dexed by trees with node size=4KB, for windows with variable size, regarding the number of disk read accesses (Table 3) and the execution time (Table 3 and Figure 5.b) vs the number of query windows are shown as one representative case. The use of a table is preferred due to the large difference of values between R^+ -tree and the other two trees. For both metrics (disk read accesses and execution time), the xBR^+ -tree has the best performance and the R^+ -tree the worst.

Studying the complete set of results (360 experiments) of *WQs*, we validate the above performance behavior. Regarding I/O:

- The number of disk read accesses per query window for the xBR⁺-tree was the smallest for the most experiments (323/360).
- For the R*-tree, it was smallest for the remainder of the experiments (37/360).

Regarding the execution time metric:

- The xBR⁺-tree had the best performance in all cases (360/360).
- The average relative difference of execution time performance between the R*-tree and the xBR+-tree is between 49.6% and 64.7%, increasing with the enlargement of the node size.
- In all trees, the execution time is reduced as the node size is increased. It is minimized for node

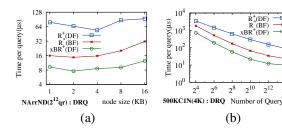


Figure 6: DRQ: exec. time vs. (a) node size (NArrND, 2^{12} query ranges) and (b) number of query ranges (500KCN with node size=4K).

size equal to 4KB, or 8KB. This is due to a tradeoff between I/O cost and CPU processing.

This behavior holds for the experiments of all datasets and all query windows.

6.5. Experiments for distance-based queries on single datasets (DRQs)

The DRQ was executed for all datasets (12) and all node sizes (5), searching for the points inside the incir- 1350 cles of the query windows, for various radius sizes (6 ε-values). Five Algorithms, N-DF, DF, S-DF, H-DF and BF, were tested for all (360) experiments. The number of disk read accesses is the same for the algorithms DF, S-DF, H-DF and BF because they all use the mindist 1355 metric and the query object is fixed. The R+-tree responded best with the algorithms using the *mindist* in all cases (360/360) in disk read accesses and faster with the DF algorithm (216/360 in execution time). The R*-tree responded best with the algorithms using the mindist in 1360 all cases (360/360) and faster with the BF algorithm in most cases (350/360 in execution time). The xBR⁺-tree responded best with the algorithms using the mindist in most cases (327/360) and faster with the DF algorithm (191/360 in execution time). So the performance com- 1365 parison for the DRQ was performed among the R⁺-tree with the DF, the R*-tree with the BF and the xBR+-tree with the DF algorithm. The results of the DRQ executed on the NArrND dataset for the 212 ranges (with $\varepsilon \leq \frac{1}{2} \times \frac{1}{\sqrt{2!^2}}$) scanning the data space are shown as a 1370 representative case. The number of disk read accesses per query (Table 4) and the execution time (Table 4 and Figure 6.a) vs node size, are depicted. The use of a table is preferred because of the large difference of values between R+-tree and the other two trees, especially for 1375 the cases of small node sizes (1KB, 2KB, 4KB).

In this table, it is shown that the xBR⁺-tree needed fewer disk read accesses (*Acc*) than the other two trees. As the node size increases, the I/O difference between the trees remains almost stable. The relative difference

Node	Disk	Read Ac	cesses	Exec	ution Tim	ne (μs)
Size	R ⁺	R*	xBR^+	R ⁺	R*	xBR^+
	(DF)	(BF)	(DF)	(DF)	(BF)	(DF)
1	46.95	8.606	8.238	78.70	15.92	9.288
2	24.47	5.441	4.769	65.47	14.72	7.585
4	11.72	3.519	3.845	53.90	15.74	8.587
8	10.07	2.825	2.410	86.92	20.17	9.034
16	5.554	2.500	2.185	93.70	31.52	12.43

Table 4: *DRQ*: disk read accesses per query on NArrND (2¹² query ranges) vs. node size.

Number	Dick	Read Ac	200000	Evec	ution Tim	a (ue)
	R ⁺	R*	xBR+	R+	R*	xBR ⁺
Query						
Points	(DF)	(BF)	(DF)	(DF)	(BF)	(DF)
2^{4}	725.5	376.5	413.0	3,463	1,822	724.3
2^{6}	303.9	106.9	108.5	1,427	516.1	191.6
2^{8}	136.6	35.43	31.30	629.3	170.0	57.80
2^{10}	65.48	14.38	10.48	295.3	66.15	21.62
2^{12}	33.69	7.721	5.090	152.1	34.14	12.00
2^{14}	18.56	5.343	4.187	87.52	22.67	9.738

Table 5: *DRQ*: disk read accesses and exec. time per query on 500KC1N (node size=4KB) vs. number of Query Ranges.

 $(Acc_{R^+} - Acc_{R^+})/Acc_{R^+}$ has values (0.82, 0.78, 0.70, 0.72, 0.55) that are all in favor of the R*-tree, while the relative difference $(Acc_{R^+} - Acc_{xBR^+})/Acc_{R^+}$ has values (0.04, 0.12, -0.09, 0.15, 0.13) that are all (except the negative one) in favor of the xBR+-tree. Note the reduction of the difference from the smallest node size (1KB) to the largest one (16KB). This is due to the reduction of the tree height as the node size increases. In Table 4 and in Figure 6.a, it is shown that the xBR+-tree is the fastest and the R*-tree is faster than the R+-tree, for all node sizes. The R+-tree needed less total execution time (I/O and CPU) with node size equal to 4KB, while the other two trees needed less execution time with node size equal to 2KB, even though larger node sizes needed fewer disk read accesses.

The results of the DRQ on the synthetic dataset 500KCN indexed by trees with node size=4KB, for various ε sizes, regarding the number of disk read accesses (Table 5) and the execution time (Table 5 and Figure 6.a) vs. the number of query ranges are shown. The xBR⁺-tree has the best performance regarding disk read accesses in most of the cases (except the one for node size=4KB) and the R⁺-tree has the worst, while the xBR⁺-tree has always the best execution time performance and the R⁺-tree the worst.

Studying the complete set of results (360 experiments) of *DRQs*, we validate the above performance behavior. Regarding I/O:

- The xBR⁺-tree had the best performance in most experiments (292/360).
- The R*-tree had the best performance in the re-

Node	Disk Read Accesses			Execution Time (µs)		
Size	R^+	R*	xBR ⁺	R^+	R*	xBR ⁺
	(BF)	(BF)	(H-DF)	(BF)	(BF)	(H-DF)
1	268.1	16.93	26.28	514.1	40.00	43.88
2	125.7	12.23	15.11	400.1	45.58	39.12
4	89.92	9.022	9.636	625.9	55.10	37.41
8	43.91	5.979	7.655	444.0	68.53	51.27
16	26.92	5.227	5.860	533.9	99.92	60.99

Table 6: K(=100) NNQ: disk read accesses per query on NArdN (2^{12} query points) vs. node size.

mainder of the experiments (68/360).

Regarding the execution time metric:

1385

1390

- The xBR⁺-tree had the best performance in all cases (360/360).
- The average relative difference of execution time 1435 performance between the R*-tree and the xBR+-tree is between 49.3% and 68.4%, increasing with the enlargement of node size.

6.6. Experiments for neighboring queries on single 1440 datasets (K-NNQs and CK-NNQs)

The KNNQ was executed for all datasets (12) and all node sizes (5), searching for the points near the centroids of the (212) query windows, for various values of K (4). Four Algorithms, DF, S-DF, H-DF and BF, 1445 were tested for all (240) experiments. The R⁺-tree responded best with the BF algorithm (222/240 in disk read accesses and 201/240 in execution time). The R*tree responded best with the BF algorithm (224/240 in disk read accesses and 239/240 in execution time). The 1450 xBR+-tree responded best with the BF algorithm in disk read accesses in most cases (166/240) and was faster with H-DF algorithm in 161/240 cases. We considered as most important criterion the execution time and selected the BF algorithm for both R-trees and the H- 1455 DF algorithm for the xBR+-tree to continue the performance comparison for KNNQs. In Figures 7.a and 7.b, we can see the results of the KNNQ with K=100 executed on the NArdN dataset for the 212 query points, distributed evenly in data space, as one representative case. The number of disk read accesses per query point 1460 and the execution time vs. the node size are shown. Because of the large difference of values between R+-tree and the other two trees, it is not easy to distinguish the differences between xBR+-tree and R*-tree. Therefore, Table 6 has been included.

In this table and in Figure 7.a, it is shown that the 1465 R*-tree needed fewer disk read accesses (Acc) than the other two trees. As the node size increases, the I/O difference between the trees decreases. The relative difference ($Acc_{R^+} - Acc_{R^+}$)/ Acc_{R^+} has values (0.94, 0.90,

0.90, 0.86, 0.81) that are all in favor of the R*-tree and the relative difference $(Acc_{R^*} - Acc_{xBR^+})/Acc_{R^*}$ has values (-0.55, -0.24, -0.07, -0.28, -0.12) that are also all in favor of the R*-tree. As the node size is increased exponentially, the number disk read accesses is reduced but not with the same ratio. For the R⁺-tree the ratio of the numbers of disk read accesses between two consecutive node sizes varies (from 0.47 up to 0.72). For the R*-tree the ratio of the numbers of disk read accesses between two consecutive node sizes presents smaller variation (from 0.66 up to 0.87) while for the xBR⁺-tree this ratio presents an intermediate level of variation (from 0.58 up to 0.79). In Table 6 and in Figure 7.b, it is shown that the xBR⁺-tree is faster than R*-tree for node sizes larger than 1KB, and the R*-tree is faster than the R+-tree, for all node sizes. All three trees have different behavior in total execution time (I/O and CPU). For the R⁺-tree, the total execution time varies without any monotony. For the R*-tree the execution time has monotonous enlargement with node size. Contrary to the previous behaviors, the xBR+-tree needed less total execution time for a node size equal to 4KB, even though larger node sizes needed fewer disk read accesses.

In Figures 7.c and 7.d, we can see the results of the KNNQ on the synthetic dataset 250KCN indexed by trees with node size=4KB, for 2^{12} query points, regarding the number of disk read accesses and the execution time vs. the value of K. The xBR^+ -tree has the best performance regarding disk read accesses looking for the 1 or 10 NNs, while R^* -tree has best performance for the 10^2 or 10^3 NNs. The R^+ -tree needed the most disk read accesses for all values of K. The xBR^+ -tree has always the best execution time performance and the R^+ -tree has the worst.

Studying the complete set of results (240 experiments for each tree) of the *KNNQ* we validate the above performance behavior:

- The number of disk read accesses per query point was the smallest for the R*-tree in most experiments (173/240).
- It was the smallest for the xBR⁺-tree in the rest of the experiments (67/240).
- Regarding the execution time metric, the xBR⁺tree had the best performance in most cases
 (209/240).
- The xBR⁺-tree has the minimum number of best performance cases in execution time with the smallest node size (26/48) and has the maximum number of best performance cases with the biggest node size (48/48).

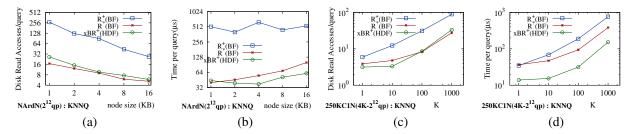


Figure 7: K(=100) NNQ: disk read accesses (a) and exec. time (b) vs. node size (NArdN, 2^{12} query points) and disk read accesses (c) and exec. time (d) vs. K values of NN (250KCN with node size=4K, 2^{12} query points).

Node	Disk Read Accesses			Execution Time (µs)		
Size	R^+	R*	xBR^+	R^+	R*	xBR^+
	(BF)	(BF)	(BF)	(BF)	(BF)	(BF)
1	20.04	4.094	4.273	36.06	10.21	6.703
2	11.83	2.977	3.128	33.58	10.65	6.389
4	8.067	2.215	2.214	40.53	12.47	7.556
8	5.113	2.169	2.135	45.50	17.72	8.641
16	4.648	2.131	2.147	77.13	50.07	13.31

Table 7: *CKNNQ*: disk read accesses per query on NArrN (2¹² query points) vs. node size.

1470

• The average relative difference of execution time performance between the R*-tree and the xBR⁺- tree in the node size of 16KB is 49.2%.

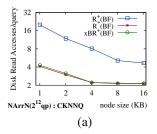
The CKNNQ was executed for all datasets (12) and all node sizes (5), searching for the points inside the incircles of the (2¹²) query windows (with $\varepsilon \leq \frac{1}{2} \times \frac{1}{\sqrt{212}}$), 1515 for various values of K (4). Four Algorithms, DF, S-DF, H-DF and BF, were tested for all (240) experiments. All the three structures responded best with the BF algorithm. In detail, the R⁺-tree responded best in 197/240 experiments in disk read accesses and in 191/240 in exe-1520 cution time. The R*-tree responded best 202/240 in disk read accesses and in 132/240 in execution time. Finally, xBR⁺-tree responded best 144/240 in disk read accesses and in 190/240 in execution time. In Figures 8.a and 8.b, we can see the results of the CKNNQ executed on 1525 the NArrN dataset for the 212 query points, distributed evenly in data space, as one representative case. The number of disk read accesses per query point and the execution time vs. the node size are shown. Because of the large difference of values between R+-tree and the other two trees, it is not easy to distinguish the differences between xBR+-tree and R*-tree. Therefore, Table 7 is depicted.

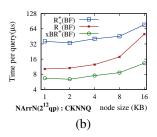
In this table and in Figure 8.a, it is shown that the R*-tree and xBR+-tree needed an almost equal number of disk read accesses (Acc). As the node size increases, the I/O difference between the trees decreases. The relative difference ($Acc_{R^+} - Acc_{R^+}$)/ Acc_{R^+} has values (0.80, 0.75, 0.73, 0.58, 0.54) that are all in favor of the R*-tree and

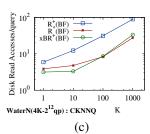
the relative difference $(Acc_{R^*} - Acc_{xBR^+})/Acc_{R^*}$ has values (-0.04, -0.05, 0.00, 0.02, -0.01), the 3 negative ones being in favor of the R*-tree. For the R+-tree the ratio of the numbers of disk read accesses between two consecutive node sizes varies widely (from 0.59 up to 0.91). For the R*-tree this ratio presents a smaller variation (from 0.73 up to 0.98) and for the xBR⁺-tree it presents a similar variation (from 0.73 up to 1.01). In Table 7 and in Figure 8.b, it is shown that the xBR+-tree is the fastest and the R*-tree is faster than the R+-tree, for all node sizes. All three trees have similar behavior in total execution time (I/O and CPU). The total execution time has monotonous increment with node size. In Figures 8.c and 8.d, we can see the results of the CKNNQ on the large real dataset Water indexed by the three trees with node size=4KB, for 2¹² query points, regarding the number of disk read accesses and execution time vs. the value of K. Because of the large number of nodes in this dataset the number of disk read accesses is quite stable for all trees. It is most stable for the R+-tree while for the other two trees varies between 1.4 and 1.8 for R*tree and 1.8 and 2.2 for the xBR+-tree. The R*-tree has the best performance regarding disk read accesses and the R⁺-tree the worst, while the xBR⁺-tree has always the best execution time performance and the R⁺-tree has

Studying the complete set of results (240 experiments for each tree) of the *CKNNQ*, we validate the above performance behavior.

- The number of disk accesses per query point for the xBR⁺-tree was the smallest in most experiments (138/240) and for the R*-tree it was the smallest in the rest of the experiments (102/240).
- Regarding the execution time metric, the xBR⁺-tree has the best performance in all the experiments (240/240).
- The average relative difference of execution time performance between the R*-tree and the xBR+-







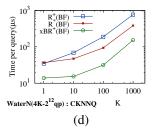


Figure 8: CKNNQ: disk read accesses (a) and exec. time (b) vs. node size (NArrN, 2^{12} query points) and read disk read accesses (c) and exec. time (d) vs. K values of NN (Water with node size=4K, 2^{12} query points).

tree is between 39.6% and 60.5%, increasing with 1575 the enlargement of the node size.

6.7. Creation of input for queries on dual datasets

In order to evaluate the performance of the trees in spatial queries where two indexes are involved (dis- 1580 tance join queries), we have used ten combinations between real and synthetic spatial datasets. Four combinations between real datasets of North America (i.e. NAppN × NArrN, NAppN × NArdN, NArrN × NArdN and NArrND × NArdND), four combinations between 1585 two separate instances of synthetic clustered datasets (i.e. $250KC1N \times 250KC2N$, $500KC1N \times 500KC2N$, $500KC1N \times 500KC2N$, and $1000KC1N \times 1000KC2N$) and two combinations between the largest real datasets (i.e. NArdND × Water and Water × Park) for query 1590 processing of the KCPQ and εDJQ . For KCPQs, the number K of closest pairs gets values from the set $\{1, 10, 10^2, 10^3, 10^4\}$ and for $\varepsilon DJQs$, the maximum distance (ε) gets values from the set $\{0, 1.25 \times 10^{-5}, 2.5 \times 1$ 10^{-5} , 5×10^{-5} , 10×10^{-5} .

6.8. Experiments for join (dual dataset) queries (KCPQs and &DJQs)

1560

In the experiments performed, the effect of LRU-buffer has also been studied, because a node of the one 1600 tree can be paired with several nodes of the other tree, in successive or not time points. Moreover, both trees corresponding to a combination of datasets were of equal node size.

6.8.1. Selection of buffer size and algorithms for the KCPQ

All combinations of datasets (10) and all node sizes (5), for various values of K (5) and with several values of LRU-buffer size (5) were used. In this series of the experiments the target was to find out for which buffer size and with which algorithm among S-DF-2, H-DF-2, C-DF-2 and C-BF-2 each tree responded better. It is obvious that as the size of the LRU-buffer increases, the

number of disk read accesses decreases and the related results will be omitted. So for the above target, only the execution time per query will be studied.

In Figure 9.a, we can see the results of the KCPQ on the combination of synthetic datasets $1000KC1N \times 1000KC2N$, both indexed by R⁺-trees with node size of 2KB, searching for the K=1000 closest pairs with all four algorithms, using LRU-buffer sizes of $0, 2^6, 2^8, 2^{10}, 2^{12}$ pages, as one representative case. It is shown that with the C-DF-2 and C-BF-2 algorithms the R⁺-tree is approximately 3 times faster than with the other algorithms for all buffer sizes. The lowest execution time value is with a buffer size of 2^{10} pages (nodes) for all algorithms and the minimum execution time value, 72,450 ms (72 sec), with the C-DF-2 algorithm

Considering the complete set of 45/50 experiments for the 5 buffer sizes (the biggest of the 10 dataset combinations, Water \times Park, was not tested for all node sizes because of the big execution time values it required), we collected the minimum execution time values for each combination and these results are shown in Table 8. It is shown that there is not a single best buffer size, neither a single best node size. We conclude that for combinations between small real datasets it is better to have no buffering, while for combinations of small synthetic and larger real datasets it is better to have buffering larger than 2^8 pages (nodes). The best algorithm for R⁺-trees executing the KCPQ is the C-BF-2 (in 9/10 cases).

In Figure 9.b, we can see the results of the KCPQ on the combination of real datasets NArdND × Water, both indexed by R*-trees with node size=2KB, searching for the K=1000 closest pairs with all four algorithms, using LRU-buffer sizes of 0, 2^6 , 2^8 , 2^{10} , 2^{12} , as one representative case. It is shown that with the C-BF-2 algorithm the R*-tree is from 1.6 up to 2 times faster than the best of the other tree algorithms for all buffer sizes. The smallest execution time value was achieved with buffer size of 0 pages (nodes) for all algorithms and the minimum execution time value, 42.418 ms, was achieved with the

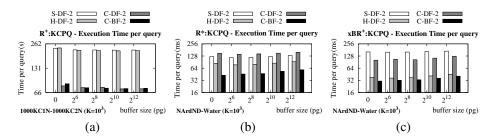


Figure 9: KCPQ with (a) R⁺-tree on $1000KC1N \times 1000KC2N$; (b) R^{*}-tree on $NArdND \times Water$; (c) xBR^+ -tree on $NArdND \times Water$: exec. time vs. buffer size per Algorithm with $K=10^3$ and node size=2KB.

Combination of datasets	Exec time (s)	Node size (KB)	Buffer size (pages)	Algo- rithm
NAppN × NArrN	0.1725	1	2^{8}	C-BF-2
$NAppN \times NArdN$	0.4091	1	0	C-DF-2
$NArrN \times NArdN$	1.0496	8	0	C-BF-2
NArrND × NArdND	1.8803	8	0	C-BF-2
250KC1N × 250KC2N	1.7793	8	2^{10}	C-BF-2
500KC1N × 500KC2N	5.6271	16	28	C-BF-2
500KC2N × 1000KC1N	12.112	16	2^{12}	C-BF-2
1000KC1N×1000KC2N	28.515	16	2^{12}	C-BF-2
NArdND × Water	342.64	16	212	C-BF-2

Table 8: $K(=10^3)$ CPQ with R⁺-tree: Min Exec Time per query for all combinations of datasets.

Combination of datasets	Exec time (ms)	Node size (KB)	Buffer size (pages)	Algo- rithm
NAppN × NArrN	56.640	2	0	C-BF-2
$NAppN \times NArdN$	136.46	4	0	C-BF-2
$NArrN \times NArdN$	157.64	1	2^{8}	C-BF-2
NArrND × NArdND	310.96	1	2^{8}	C-BF-2
250KC1N × 250KC2N	206.93	4	2^{6}	C-BF-2
500KC1N × 500KC2N	405.03	4	2^{6}	C-BF-2
500KC2N×1000KC1N	599.60	8	2^{6}	C-BF-2
1000KC1N×1000KC2N	845.10	16	0	C-BF-2
NArdND × Water	30.255	1	0	C-BF-2
Water × Park	1,031.9	4	0	C-BF-2

Table 9: $K(=10^3)$ CPQ with R*-tree: Min Exec Time per query for all combinations of datasets.

C-BF-2 algorithm.

Considering the complete set of all (50) experiments for the 10 dataset combinations and 5 buffer sizes, we collected the minimum execution time values for each combination. These results are shown in Table 9. It is shown that R*-tree responded best in half of the cases (5/10), including the combination between large real datasets, without buffering, while in the 4 combinations with synthetic datasets it responded best with 2⁶ pages in LRU-buffer (in 3/4 cases). The best algorithm for R*-trees executing the *KCPQ* is the C-BF-2.

Finally, in Figure 9.c, we can see the results of the KCPQ on the combination of real datasets NArdND × Water, both indexed by xBR⁺-trees with node size=2KB, searching for the K=1000 closest pairs, 1655

Combination of datasets	Exec time (ms)	Node size (KB)	Buffer size (pages)	Algo- rithm
NAppN × NArrN	17.302	16	0	C-DF-2
$NAppN \times NArdN$	34.306	4	0	H-DF-2
$NArrN \times NArdN$	57.432	8	0	C-BF-2
NArrND × NArdND	114.51	16	0	C-BF-2
250KC1N × 250KC2N	42.111	4	0	C-BF-2
500KC1N × 500KC2N	71.459	8	0	C-BF-2
500KC2N × 1000KC1N	99.164	8	0	C-BF-2
1000KC1N×1000KC2N	124.28	8	0	C-BF-2
NArdND × Water	30.706	2	0	C-BF-2
Water \times Park	473.56	4	0	C-BF-2

Table 10: $K(=10^3)$ CPQ with xBR⁺-tree: Min Exec Time per query for all combinations of datasets.

with all four algorithms, using LRU-buffer sizes of $0, 2^6, 2^8, 2^{10}, 2^{12}$, as one representative case. It is shown that with the C-BF-2 algorithm the xBR⁺-tree is from 3.0 up to 3.3 times faster than the best of the S-DF-2 and C-DF-2 algorithms and from 1.1 up to 1.2 faster than the H-DF-2 algorithm for all buffer sizes. The lowest execution time value was achieved with buffer size of 0 pages (nodes) for all algorithms and the minimum execution time value, 30.706 ms, was achieved with the C-BF-2 algorithm.

Considering the complete set of all (50) experiments for the 10 dataset combinations and 5 buffer sizes, we collected the minimum execution time values for each combination and these results are shown in Table 10. It is shown that xBR⁺-tree responded best in all the cases (10/10) without buffering. The best algorithm for xBR⁺-trees executing the *KCPQ* was the C-BF-2 (in 8/10 cases).

In conclusion, we note that:

- There is no meaning for a comparison between the R⁺-tree and the other two trees because of the very large difference in execution times observed (the R⁺-tree was mainly designed for *PLQs* and *WQs*).
- Based on the above results, we continue the performance comparison between the R*-tree and xBR+-tree, using the C-BF-2 algorithm for both trees

without LRU-buffer (0 pages) for all node sizes, for various values of K (1, 10, 10^2 , 10^3 and 10^4) and for both performance metrics (i.e. the number of disk read accesses and the execution time).

6.8.2. Performance study of the KCPQ

In Figures 10.a and 10.b, we can see the results of the KCPQ with $K = 10^3$, executed on the combination of large real datasets Water × Park, as one representative case. The number of disk read accesses per query point and the execution time vs. the node size are shown. The xBR⁺-tree needed fewer disk read accesses (Acc) than the R*-trees having node sizes between 2KB and 8KB. As the node size increases, the ratio of the I/O difference between the two trees varies. The relative difference 1705 $(Acc_{R^*} - Acc_{RR^+})/Acc_{R^*}$ has values (-1.59, 0.22, 0.20, 0.12, -0.23), the 3 positive one being in favor of the xBR+-tree. For the R*-tree, the ratio of the numbers of disk read accesses between two consecutive node sizes presents a small variation (from 0.5 up to 0.6) and is al- $_{\mbox{\tiny 1710}}$ ways decreased. For the xBR+-tree, this ratio presents a similar variation from 0.6 up to 0.8 (except the first case from 1 to 2 KB where it is 0.2). In Figure 10.b, it is shown that the xBR+-tree is faster than R*-tree for all node sizes bigger than 1KB. For both trees the execution time has a minimum value with a node size of 4KB, even though larger node sizes needed fewer disk read accesses. In Figures 10.c and 10.d, we can see the results of the KCPQ on the same combination of large real datasets indexed by trees with node size of 4KB, $_{\scriptscriptstyle 1720}$ regarding the number of disk read accesses and the execution time vs. the value of K. The number of disk read accesses needed by both trees remains stable although the number of *K* is increased exponentially. The xBR^{+} -tree has the best performance regarding disk read accesses in all the cases.

Studying the complete set of results (250 experiments for each tree) for the *KCPQ*, we validate the above performance behavior.

The number of disk accesses per query for the ¹⁷³⁰ xBR⁺-tree was the smallest for most experiments (224/250).

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- The xBR⁺-tree was faster than the R*-tree in all experiments with node sizes of 2KB and 16KB, in ¹⁷³⁵ 46/50 cases with node size of 4KB, while, in total, it was faster in 231/250 cases.
- The average relative difference of execution time performance between the R*-tree and the xBR+- 1740 tree is between 62.7% and 71.9%.

Combination of datasets	Exec time (ms)	Node size (KB)	Buffer size (pages)	Algo- rithm
NAppN × NArrN	0.146	1	2^{10}	H-DF-2
$NAppN \times NArdN$	0.347	1	0	H-DF-2
$NArrN \times NArdN$	0.873	1	2^{10}	H-DF-2
NArrND × NArdND	2.085	1	2^{10}	H-DF-2
250KC1N × 250KC2N	5.994	1	28	H-DF-2
500KC1N × 500KC2N	25.16	1	2^{8}	H-DF-2
500KC2N × 1000KC1N	29.98	1	2^{10}	H-DF-2
1000KC1N×1000KC2N	55.97	1	2^{8}	H-DF-2
NArdND × Water	2,202	4	2^{10}	C-BF-2

Table 11: εDJQ ($\varepsilon = 1.25 \times 10^{-5}$) with R⁺-tree: Min Exec Time per query for all combinations of datasets.

6.8.3. Selection of buffer size and algorithms for the εDJQ

For the εDJQ the same scenario of experiments to the one of KCPQ was performed to find out for which buffer size and with which algorithm among S-DF-2, H-DF-2, C-DF-2 and C-BF-2 each tree responded better, regarding the execution time metric.

In Figure 11.a, we can see the results of the εDJQ on the combination of synthetic datasets $1000KC1N \times 1000KC2N$, both indexed by R⁺-trees, with node size of 4KB, searching for the pairs with distance $\leq 1.25 \times 10^{-5}$ with all four algorithms, using LRU-buffer sizes of $0, 2^6, 2^8, 2^{10}, 2^{12}$ pages, as one representative case. We chose to present the same dataset combinations to the previous query (KCPQ) because of the similarity which exists between the two types of queries. It is shown that with the C-DF-2 algorithm the R⁺-tree is slightly faster than with the other algorithms for all buffer sizes. The lowest execution time value is achieved with buffer size of 2^{10} pages (nodes) for all algorithms and the minimum execution time value, 152,541 ms (152 sec), is achieved with the C-DF-2 algorithm.

Considering the complete set of 45/50 experiments for the 5 buffer sizes (the biggest combination Water×Park was not tested for all node sizes because of the big execution time values) we collected the minimum execution time values for each combination and these results are shown in Table 11. It is shown that there is not a single best buffer size, while 9/10 best execution times were achieved with node size equal to 1KB. We conclude that for combinations between small real datasets it is better to have 2^{10} pages in LRU-buffer, while for combinations of small synthetic and large real datasets it is better to have 2^8 buffer pages (nodes). The best algorithm for R⁺-trees executing the εDJQ is the H-DF-2 (in 9/10 cases).

In Figure 11.b, we can see the results of the εDJQ on the combination of real datasets NArdND × Water, both

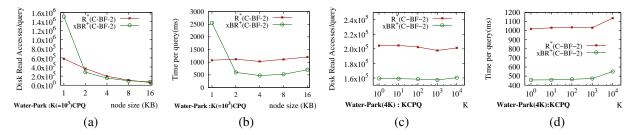


Figure 10: KCPQ on large real datasets Water \times Park: disk read accesses (a) and exec. time (b) vs. node size $(K=10^3)$ and disk read accesses (c) and exec. time (d) vs. K values of CP (node size=4K).

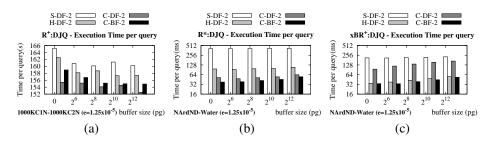


Figure 11: εDJQ with (a) R⁺-tree on 1000KC1N × 1000KC2N; (b) R^{*}-tree on NArdND × Water; (c) xBR⁺-tree on NArdND × Water: exec. time vs. buffer size per Algorithm with $\varepsilon = 1.25 \times 10^{-5}$ and node size=4KB.

indexed by R*-trees with node size of 4KB, searching for the pairs with distance $\leq 1.25 \times 10^{-5}$ with the four algorithms, using LRU-buffer sizes of $0, 2^6, 2^8, 2^{10}, 2^{12}$ pages, as one representative case. It is shown that with the C-BF-2 algorithm the R*-tree is from 1.1 up to 1.4 times faster than the best of the other tree algorithms for all buffer sizes. The lowest execution time value is achieved with buffer size of 0 pages (nodes) for all algorithms and the minimum execution time value, 37.837 ms, is achieved with the C-BF-2 algorithm.

Considering the complete set of all (50) experiments for the 10 dataset combinations and 5 buffer sizes, we collected the minimum execution time values for each combination and these results are shown in Table 12. It is shown that R*-tree responded best in half cases (5/10), including the combinations between large real datasets, without buffering, while in the 4 combinations between synthetic datasets it responded best with 2^6 pages in 1775 LRU-buffer (in 3/4 cases). The best algorithm for R*-trees executing the εDJQ is the C-BF-2.

Finally, in Figure 11.c, we can see the results of the εDJQ on the combination of real datasets NArdND×Water, both indexed by xBR⁺-trees with 1780 node size of 4KB, searching for the pairs with distance $\leq 1.25 \times 10^{-5}$ with all four algorithms, using LRU-buffer sizes of $0, 2^6, 2^8, 2^{10}, 2^{12}$ pages, as one representative case. It is shown that with the C-BF-2 algorithm the xBR⁺-tree is from 2.8 up to 3.5 times faster than the best among the S-DF-2 and C-DF-2 algorithms and 1785

Combination of datasets	Exec time (ms)	Node size (KB)	Buffer size (pages)	Algo- rithm
NAppN × NArrN	50.619	4	0	C-BF-2
$NAppN \times NArdN$	129.48	4	0	C-BF-2
$NArrN \times NArdN$	157.00	1	2^{8}	C-BF-2
NArrND × NArdND	319.55	1	2^{8}	C-BF-2
250KC1N × 250KC2N	176.06	8	2^{6}	C-BF-2
500KC1N × 500KC2N	356.79	16	2^{6}	C-BF-2
500KC2N × 1000KC1N	532.82	16	0	C-BF-2
1000KC1N×1000KC2N	782.53	16	2^{6}	C-BF-2
NArdND × Water	25.698	1	0	C-BF-2
Water × Park	1,212.5	4	0	C-BF-2

Table 12: εDJQ ($\varepsilon=1.25\times 10^{-5}$) with R*-tree: Min Exec Time per query for all combinations of datasets.

from 1.03 up to 1.13 faster than the H-DF-2 algorithm for all buffer sizes. The lowest execution time value was achieved with buffer size of 2⁶ pages (nodes) for all algorithms and the minimum execution time value, 33.437 ms, was achieved with the C-BF-2 algorithm.

Considering the complete set of all (50) experiments, we collected the minimum execution time values for each combination of datasets and these results are shown in Table 13. It is shown that xBR^+ -tree responded best without buffering in all combinations of datasets. The best algorithm for xBR^+ -trees executing the εDJQ is the H-DF-2 (8/10 cases).

In conclusion, we note that:

• There is no meaning for a comparison between the R^+ -tree and the other two trees for εDJQ , because

Combination of datasets	Exec Time(s)	Node size	Buffer size	Algo- bfrithm
NAppN × NArrN	11.094	16	0	H-DF-2
$NAppN \times NArdN$	27.156	4	0	H-DF-2
$NArrN \times NArdN$	46.244	4	0	H-DF-2
NArrND × NArdND	119.86	2	0	H-DF-2
250KC1N×250KC2N	21.346	16	0	C-BF-2
500KC1N × 500KC2N	47.708	8	0	H-DF-2
500KC2N×1000KC1N	73.090	8	0	H-DF-2
1000KC1N×1000KC2N	102.57	8	0	H-DF-2
NArdND × Water	23.360	2	0	C-BF-2
Water × Park	682.02	4	0	H-DF-2

Table 13: εDJQ ($\varepsilon = 1.25 \times 10^{-5}$) with xBR⁺-tree: Min Exec Time per query for all combinations of datasets.

of the very big difference in execution times observed (the R^+ -tree was mainly designed for PLQs and WQs).

• We continue the performance comparison between the R*-tree and xBR+-tree, using the C-BF-2 algorithm for the first one and the H-DF-2 algorithm for the second one, without LRU-buffer (0 pages) for all node sizes, for various values of $\varepsilon(0, 1.25 \times 10^{-5}, 2.5 \times 10^{-5}, 5 \times 10^{-5}, 10 \times 10^{-5})$ and for both performance metrics (i.e. the number of disk read accesses and the execution time).

6.8.4. Performance study of the εDJQ

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In Figures 12.a and 12.b, we can see the results of the 1845 εDJQ with $\varepsilon = 1.25 \times 10^{-5}$ executed on the combination of large real datasets Water × Park, as one representative case. The number of disk read accesses per query and the execution time vs. the node size are shown. The xBR⁺-tree needed fewer disk read accesses (Acc) than the R*-tree for all node sizes. As the node size increases, the ratio of the I/O difference between the two trees varies. The relation between I/O performance and the node size is quite stable (almost linear). The relative difference $(Acc_{R^*} - Acc_{xBR^+})/Acc_{R^*}$ has values (0.76, 0.71, 0.66, 0.61, 0.49), all in favor of the xBR⁺-tree. For the R*-tree, the ratio of the numbers of disk read 1855 accesses between two consecutive node sizes presents a small variation (from 0.42 up to 0.49 and always is decreased) and for the xBR+-tree this ratio presents a similar level of variation, from 0.51 up to 0.60. In Figure 12.b, it is shown that the xBR+-tree is faster than 1860 the R*-tree for all node sizes. For both trees the execution time has minimum value with node size of 4KB, even though larger node sizes needed fewer disk read accesses. In Figures 12.c and 12.d, we can see the results of the εDJQ on the same combination of large real 1865 datasets indexed by trees with node size of 4KB, regarding the number of disk read accesses and the execution time vs. the value of ε . The number of disk

read accesses needed by xBR^+ -tree remains very stable although the value of ε is increased exponentially. The xBR^+ -tree has the best performance regarding disk read accesses in the most cases (3/5), while in the execution time it was the best in all cases.

Studying the complete set of results (250 experiments for each tree) for the εDJQ , we validate the above performance behavior.

- The number of disk accesses per query for the xBR⁺-tree was the smallest for most experiments (216/250).
- The xBR⁺-tree was faster than the R*-tree in all experiments with node sizes 2KB and 4KB, in 49/50 cases with node size of 16KB, while in total it was faster in 235/250 case.
- The average relative difference of execution time performance between the R*-tree and the xBR+-tree is between 66.2% and 68.2%.

6.9. Summary and conclusions of experimental results

The experimental results of tree building are summarized in the following.

- The xBR⁺-tree needs a little less space (in most cases) and is built in a smaller time than the two R-trees.
- The xBR⁺-tree building is faster than the R*-tree and the R*-tree is faster than R⁺-tree for all datasets and node sizes.
- This difference is increasing as the node size increases and becomes bigger for the large real datasets.

The fractions of cases where the xBR⁺-tree is an execution time and I/O performance winner, for each (single, or dual dataset) query, is depicted in Table 14. The second and third columns refer to the aggregate results for all page sizes, while the fourth and sixth columns refer to results when using a page size of 16KB. The fifth column refers to the xBR⁺-tree gain in execution time, (R*-tree exec. time – xBR⁺-tree exec. time) / R*-tree exec. time, for the page size of 16KB (e.g. a gain value equal to 66.67% for a query means that the xBR⁺-tree needs 1/3 of the execution time of the R*-tree to answer this query). By studying these results, we conclude that the xBR⁺tree is a clear performance winner, in relation to the R*-tree (the best among R-trees). More specifically:

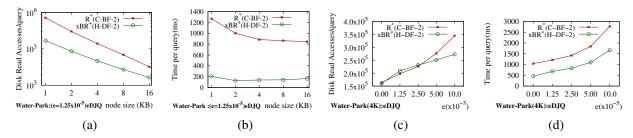


Figure 12: εDJQ on large real datasets Water×Park: disk read accesses (a) and exec. time (b) vs. node size ($\varepsilon = 1.25 \times 10^{-5}$) and disk read accesses (c) and exec. time (d) vs. ε values (node size=4KB).

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Query	all noc	all node sizes		node size=16KB			
name	Time	I/O	Time	gain	I/O		
Single-dat	aset queries	:					
\overline{WQ}	360/360	323/360	72/72	64.7%	68/72		
DRQ	360/360	292/360	72/72	68.4%	67/72		
KNNQ	209/240	67/240	48/48	49.2%	18/48		
CKNNQ	240/240	138/240	48/48	60.5%	30/48		
Dual-data	set queries:						
KCPQ	231/250	224/250	50/50	71.9%	45/50		
εDJO	235/250	216/250	49/50	66 4%	43/50		

Table 14: Synopsis of efficiency of xBR+-tree in all queries vs. R*-tree

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- The xBR⁺-tree is a big winner in execution time in all cases and a winner in I/O in all cases except of the I/O of the KNNQ.
- The xBR⁺-tree is an almost absolute winner when the page size equals 16KB (for this page size the xBR⁺-tree is a relative winner in the I/O of the *KNNQ*, too). Note the high percentages of gain for this page size.

Note that the R⁺-tree was designed specifically for PLQs and WQs and not for other ones, like DRQs, KNNQs, KCPQs, $\varepsilon DJQs$, etc.

The regular subdivision of space, the additional representation of the minimum rectangles bounding the actual data objects (DBRs), the extra termination condition applicable in certain queries and the storage order of the entries of internal nodes gave the ability to the xBR⁺-tree to be a more efficient structure than R-trees and even than the R*-tree. More specifically, the building performance of the xBR⁺-tree can be credited to the following:

• Due to the regular subdivision of space, the calculations needed are much fewer and simpler than ¹⁹²⁵ those of the R*-tree.

The building time of an xBR⁺-tree is smaller even than the one needed for building the respective, very simple, R⁺-tree. The very good performance of the xBR⁺-tree in queries can be credited to the following:

- The regular subdivision of space leads to laying the (sub)quadrants, created by the data distribution, in the corners of the embedding (sub)space.
 In this way, the distances between them are maximized and pruning during join query processing is increased.
- Due to the quadrangular shape of the (sub)quadrants, the dimensions of the contained DBRs are minimized. The minimal dimensions of DBRs in conjunction with their laying in the corners of the embedding (sub)space allows the high exploitation of metrics like *mindist* (the R⁺-trees, due to their structure, do not utilize efficiently such pruning techniques).
- In xBR⁺-trees, DBRs are expoited as an extra tool of delimiting the subspace containing data objects.
- By examing the entries of an xBR⁺-tree internal node in reverse preorder traversal of the Quadtree that corresponds to this internal node (a subregion is examined before any enclosing region of this subregion), multiple examinations of overlapping regions are avoided (at least in point location and window queries).
- The disjointness between regions and the combination of the region of each node with the *Shape* property of this node gives the ability of an extra termination condition in window and range queries (this condition cannot be applied in R-trees, due to their structure).

The conclusions arising from the performance results of the alternative DF/BF algorithms for processing queries are summarized in the following:

• For *PLQs* and *WQs*, N-DF algorithms are the only applicable, since the criterion for such queries is boolean (true/false).

Query	R	+-tree	R	*-tree	xBl	R ⁺ -tree	١.
Name	(%)	Alg	(%)	Alg	(%)	Alg	
Single-dataset queries:							
DRQ	69.2	DF	75.3	DF	54.4	DF	
KNNQ	64.6	S-DF	81.7	H-DF	99.2	H-DF	
CKNNQ	64.6	H-DF	65.8	H-DF	51.7	H-DF	
Dual-data	set quer	ies:					
KCPQ	90.0	C-DF-2	54.8	H-DF-2	95.6	H-DF	
εDJQ	44.8	C-DF-2	99.6	C-DF-2	95.6	H-DF-2	1

Table 15: The winning DF algorithm (and the respective percentage of cases) for *DROs*, *KNNOs*, *CKNNOs*, *KCPOs*, and ε*DJOs*.

- For the rest of the queries, among DF algorithms, 1980 the winning algorithm and the respective percentage of cases is depicted in Table 15. It is obvious that the H-DF variants are the most efficient ones in xBR⁺-trees, in 4/5, and in R*-trees, in 3/5 of the query types. As noted in Subsection 5.1, this is 1985 due to partial sorting of (pairs of) entries by *mindist* when H-DF variants are used.
- BF algorithms perform significantly better on the R*-tree, since, due to overlapping between regions of nodes at the same level, the minimization of I/O that BF algorithms achieve plays an important role. 1990

7. Conclusions and Future Work

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In [18], the xBR⁺-tree was compared to the xBR-tree for single dataset queries and datasets of medium size and "a detailed relative performance study of the xBR⁺-tree against the R*-tree and/or R⁺-tree for single dataset and multi-dataset queries" was mentioned as the main future work target, since these structures had never been compared in the literature.

In this paper, we accomplished this target based on single, as well as, on dual dataset queries, utilizing existing and new algorithms and performing experiments on medium, as well as, large datasets. More specifically, in this paper, we presented algorithms for PLQs and WQs used in the above three structures. We also presented for these structures N-DF, S-DF and BF existing algorithms and the new H-DF algorithm for DRQs, KNNQs and CKNNQs. Moreover, we presented the first algorithms for KCPQs and $\varepsilon DJQs$ on the xBR⁺-tree and a new alternative DF algorithm (H-DF-2) for KCPQs and $\varepsilon DJQs$ for all the three trees. We also highlighted the differences between alternative algorithms.

Moreover, by a detailed performance comparison (I/O and execution time) of xBR^+ -trees (non-overlapping trees of the quadtree family), R^+ -trees (non-overlapping trees of the R-tree family) and R^* - ²⁰¹⁵ trees (industry standard belonging to the R-tree family) for tree building, processing single point dataset

queries (*PLQs*, *WQs*, *DRQs*, *KNNQs* and *CKNNQs*) and distance-based join queries (*KNNQs*, *\varepsilon DJQs*), using medium and large spatial (real and synthetic) datasets, we showed that the xBR⁺-tree is a clear winner in tree building, a big winner in execution time in all cases and a winner in I/O in all cases, except for the I/O of the *KNNQ* (it is an almost absolute winner when the page size equals 16KB).

The building performance of the xBR⁺-tree is due to the regular subdivision of space that leads to much fewer and simpler calculations. The higher query performance of the xBR⁺-tree is due to the combination of the regular subdivision of space, the additional representation of the minimum rectangles bounding the actual data objects (DBRs) and the extra termination condition applicable in certain queries and the storage order of the entries of internal nodes gave

In the future we plan to:

- Compare the three trees for data of dimensionality larger than 2,
- Create extensions of the xBR⁺-tree for non-point data objects and algorithms for processing queries on them and compare to competitive structures,
- Create extensions of the xBR⁺-tree for parallel and distributed environments,
- Create algorithms to bulk-load xBR+-trees.

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